

Please write clearly in block capitals.

Centre number

Candidate number

Surname _____

Forename(s) _____

Candidate signature _____

I declare this is my own work.

GCSE MATHEMATICS

H

Higher Tier Paper 2 Calculator

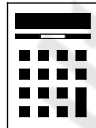
Wednesday 4 June 2025

Morning Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper.
- These must be tagged securely to this answer book.

Advice

In all calculations, show clearly how you work out your answer.

For Examiner's Use	
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
TOTAL	



Answer **all** questions in the spaces provided.

- 1 (a) Work out the highest common factor (HCF) of 16 and 24

[1 mark]

$$\begin{array}{r}
 16 \\
 \swarrow \searrow \\
 (2) \quad 8 \\
 \swarrow \searrow \\
 (2) \quad 4 \\
 \swarrow \searrow \\
 (2) \quad (2)
 \end{array}
 \qquad
 \begin{array}{r}
 24 \\
 \swarrow \searrow \\
 (2) \quad 12 \\
 \swarrow \searrow \\
 (2) \quad 6 \\
 \swarrow \searrow \\
 (2) \quad (3)
 \end{array}
 \qquad
 \begin{array}{l}
 16 = \boxed{2} \times \boxed{2} \times \boxed{2} \times 2 \\
 24 = \boxed{2} \times \boxed{2} \times \boxed{2} \times 3 \\
 \text{HCF} = 2 \times 2 \times 2 = 8
 \end{array}$$

Answer 8

- 1 (b) Work out the lowest common multiple (LCM) of 10 and 15

[1 mark]

$$\begin{array}{r}
 10 \\
 \swarrow \searrow \\
 (2) \quad (5)
 \end{array}
 \qquad
 \begin{array}{r}
 15 \\
 \swarrow \searrow \\
 (3) \quad (5)
 \end{array}
 \qquad
 \begin{array}{l}
 10 = 2 \times \boxed{5} \\
 15 = 3 \times \boxed{5} \\
 \text{LCM} = 5 \times 2 \times 3
 \end{array}$$

Answer 30

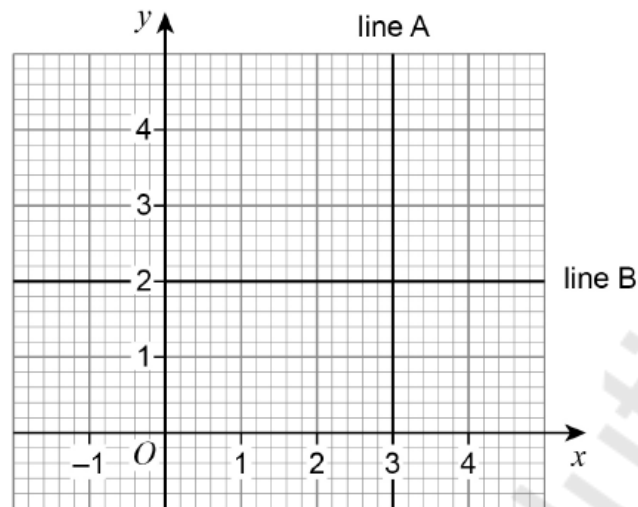
- 1 (c) Write 42 as a product of its prime factors.

[1 mark]

$$\begin{array}{r}
 42 \\
 \swarrow \searrow \\
 21 \quad (2) \\
 \swarrow \searrow \\
 (3) \quad (7)
 \end{array}$$

Answer $2 \times 3 \times 7$ 

2 Here are lines A and B.



Complete these statements.

[2 marks]

The **equation** of line A is $x = 3$

The **gradient** of line B is 0

Turn over for the next question



3

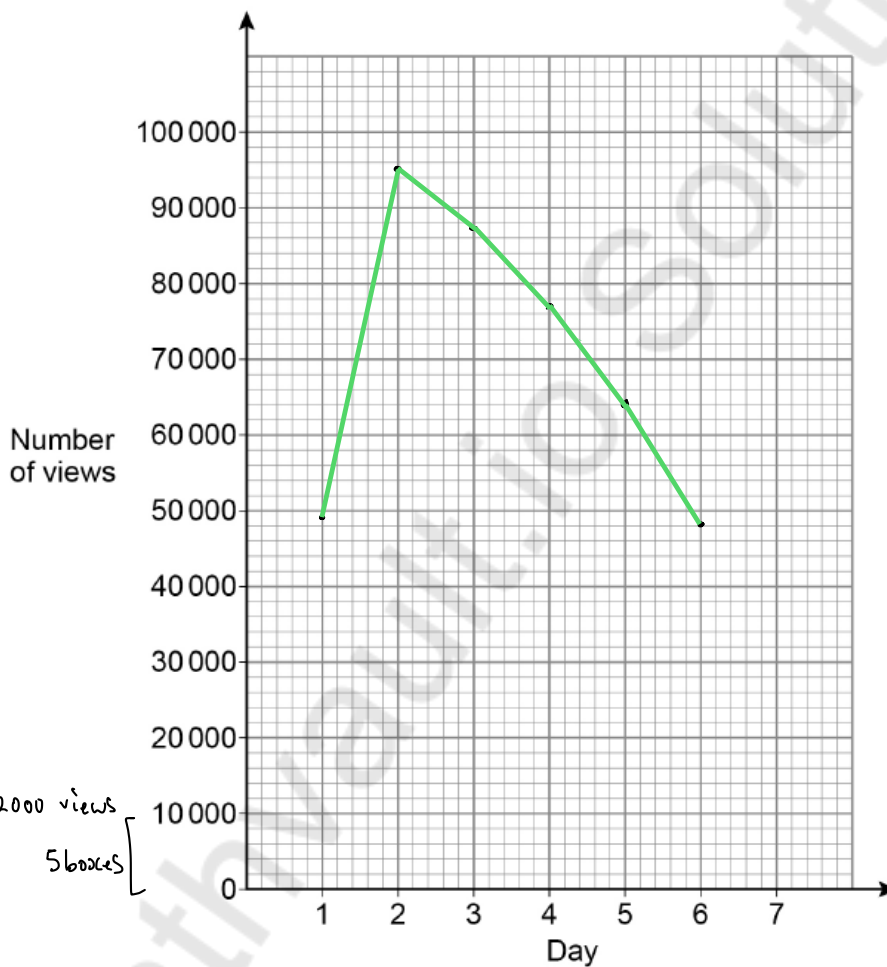
Youssuf posted an advert on his social media channel.

The table shows the number of views of the advert during its first 6 days.

Day	1	2	3	4	5	6	7
Number of views	49 000	95 000	87 000	77 000	64 000	48 000	29 000
			-8 000	-10 000	-13 000	-16 000	-19 000

3 (a) On the grid, draw a time series graph to represent the data.

[2 marks]



- 3 (b) Youssuf receives 0.018p for each view of the advert.
Estimate how much he receives from views of the advert on **day 7**

[3 marks]

$$\begin{aligned} \text{Money for Day 7} &= 29000 \times 0.018p = 522p \\ 522p &\div 100 = \pounds 5.22 \end{aligned}$$

Answer £ 5.22

- 4 70% of the discs in a box are red and the rest are blue.

- 40% of the red discs are removed.
- 50% of the blue discs are removed.

In total, what percentage of the discs are removed from the box?

[3 marks]

Assume total number of discs = x

$$\text{Blue} = 0.3x$$

$$\text{Red} = 0.7x$$

$$\text{Red removed} = 0.4 \times 0.7x = 0.28x$$

$$\text{Blue removed} = 0.5 \times 0.3x = 0.15x$$

$$0.43x = \text{Total removed}$$

Answer 43 %

Turn over ►



- 7 The five possible outcomes of an event are A, B, C, D and E.
The table shows some of the probabilities.

Outcome	A	B	C	D	E
Probability	0.18	0.2	0.3	0.16	0.16

$$P(C) = P(B) + 0.1$$

$$P(D) = P(E) = x$$

Work out $P(D)$

[3 marks]

$$P(C) = 0.2 + 0.1 = 0.3$$

$$0.18 + 0.2 + 0.3 + x + x = 1$$

$$\begin{array}{r} 0.68 + 2x = 1 \\ -0.68 \quad -0.68 \end{array}$$

$$2x = 0.32$$

$$\div 2 \quad \div 2$$

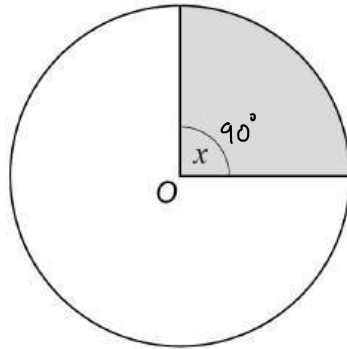
$$x = 0.16$$

Answer 0.16

Turn over for the next question



- 8 Here is a circle, centre O.



Not drawn
accurately

- 8 (a) The circle has a circumference of 20 cm

Assume that angle x is 90°

Work out the shaded area.

Give your answer as a decimal.

[3 marks]

$$C = \pi \times D$$

$$\text{Area} = \frac{\theta}{360} \times \pi r^2$$

$$20 = \pi \times D$$

$$\text{Area} = \frac{90}{360} \times \pi \times \left(\frac{10}{\pi}\right)^2$$

$$\frac{20}{\pi} = D$$

$$= \frac{1}{4} \times \pi \times \frac{100}{\pi^2}$$

$$r = \frac{1}{2} \times D$$

$$\text{Area} = \frac{25}{\pi} \text{ cm}^2$$

$$r = \frac{1}{2} \times \frac{20}{\pi}$$

$$r = \frac{10}{\pi} \text{ cm}$$

Answer 7.96 cm²



8 (b) In fact, angle x is smaller than 90°



What does this mean about the shaded area?

Tick **one** box.

[1 mark]

It is smaller than the answer to part (a)

It is the same as the answer to part (a)

It is larger than the answer to part (a)

It could be any of the above

9 The number of people that follow an influencer increases from 35 000 to 70 000

The influencer says,

“My number of followers has increased by 200%, because 70 000 is 35 000 times 2”

Are they correct?

Tick a box.

Yes

No

Give a reason for your answer.

[1 mark]

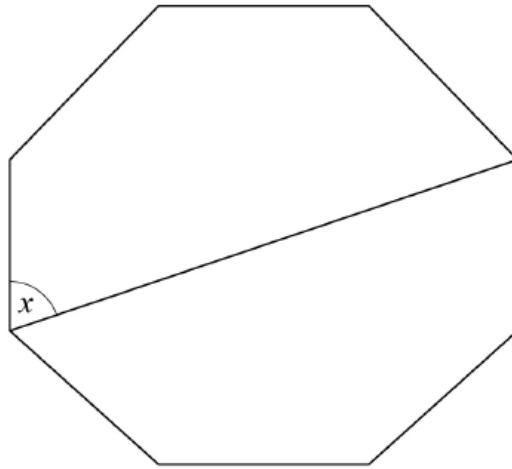
Number of followers actually increased by
100% not 200%

$$\% \text{ increase} = \frac{35000}{35000} \times 100 = 100\%$$



- 11 A straight line is drawn across a **regular** octagon.
 $n = 8$

Not drawn
accurately



Work out the size of angle x .

[3 marks]

$$(n-2) \times 180 = \text{Sum of interior angles}$$

$$(8-2) \times 180$$

$$6 \times 180$$

$$1080^\circ$$

$$\text{One interior angle} = \frac{1080}{8} = 135^\circ$$

$$x = 135^\circ \div 2 = 67.5^\circ$$

$$x = 67.5^\circ$$



12 Greg and Hanna want to know if students at their school think lunchtime clubs are important.

12 (a) Greg asks 15 people at the lunchtime chess club.

Give **one** reason why his results may **not** represent the whole school.

[1 mark]

Only Students at chess club were asked so the
Sample / Survey is biased.

12 (b) Here are Hanna's results.

- 62% answered Important.
- 24% answered Not Important.
- The rest answered Don't Know.

93 students answered Important.

How many students answered Don't Know?

Percentage % No of Students

$$\% \text{ of don't know} = 100\% - 62\% - 24\%$$

$$\% \text{ of don't know} = 14\%$$

[3 marks]

$$\begin{array}{l} 62\% : 93 \\ \div 62 \\ 1\% : 1.5 \\ \times 14 \\ 14\% : 21 \end{array}$$

Answer

21



13

Emma and Chan each drive 154 miles from A to B.

Emma drives the whole way at an average speed of 56 miles per hour.

Chan drives

85 miles at an average speed of 50 miles per hour

and then

the rest of the way at an average speed of 60 miles per hour.

Who takes **less** time, Emma or Chan?

Show working to support your answer.

[4 marks]

$$\text{Time for Emma} = \frac{154}{56} = 2.75 \text{ hours} \quad 154 - 85$$

$$\text{Time for Chan (part 1)} = \frac{85}{50} = 1.7 \text{ hours} \quad 69 \text{ miles}$$

$$\text{Time for Chan (part 2)} = \frac{69}{60} = 1.15 \text{ hours}$$

$$\text{Total time for Chan} = 2.85 \text{ hours}$$

$$2.75 < 2.85 \quad \text{So Emma takes less time}$$

Answer

Emma

Do not write
outside the
box

Turn over ►



14 a , b and c are positive integers.

$$a(9x + 2) \equiv 45x + 3b + c$$

Work out **one** possible set of values for a , b and c .

[3 marks]

$$9ax + 2a \equiv 45x + 3b + c$$

$$\begin{array}{l} 9a = 45 \\ \div 9 \end{array}$$

$$2a = 3b + c$$

$$2(5) = 3b + c$$

$$a = 5$$

$$10 = 3b + c$$

$$10 = 9 + 1 \quad c = 1$$

$$3b = 9$$

$$\div 3$$

$$\div 3$$

$$b = 3$$

$$a = \underline{5} \quad b = \underline{3} \quad c = \underline{1}$$



15 Solve $3x^2 + 5x - 9 = 0$

Give your solutions as decimals.

[2 marks]

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad a = 3, b = 5, c = -9$$

$$x = \frac{-5 \pm \sqrt{(5)^2 - 4(3)(-9)}}{2(3)}$$

$$x = \frac{-5 \pm \sqrt{133}}{6}$$

$$x = \frac{-5 + \sqrt{133}}{6} \quad x = \frac{-5 - \sqrt{133}}{6}$$

$$x \approx 1.09 \text{ (3 s.f.)} \quad x \approx -2.76 \text{ (3 s.f.)}$$

Answer 1.09 and -2.76

16 The value of a second-hand car decreases by 12.1% per year.

Work out the number of full years until the car loses **more** than half its value.You **must** show your working.

[3 marks]

Assume value of car is x

$$100\% - 12.1\% = 87.9\% = 0.879$$

$$\text{After 1 year} = 0.879x$$

$$\text{After 2 years} = 0.879 \times 0.879x = 0.773x \text{ (3sf)}$$

$$\text{After 3 years} = 0.879^3 x = 0.679x \text{ (3sf)}$$

$$\text{After 4 years} = 0.879^4 x = 0.597x \text{ (3sf)}$$

$$\text{After 5 years} = 0.879^5 x = 0.525x \text{ (3sf)}$$

$$\text{After 6 years} = 0.879^6 x = 0.461x \text{ (3sf)}$$

Answer 6 years

Turn over ►



17

When a biased coin is spun, $P(\text{Heads}) : P(\text{Tails}) = \underbrace{5 : 2}_{7 \text{ total}}$

In a game, the player spins the coin four times.

The player can win in **two** ways.

1st way to win

Spin 4 heads

2nd way to win

Spin a Head, then a Tail, then a
Head, then a Tail

How many times more likely is a player to win the 1st way than the 2nd way?

[3 marks]

$$P(H) = \frac{5}{7}$$

$$P(T) = \frac{2}{7}$$

$$P(\text{1st way win}) = \frac{5}{7} \times \frac{5}{7} \times \frac{5}{7} \times \frac{5}{7} = \frac{625}{2401}$$

$$P(\text{2nd way win}) = \frac{5}{7} \times \frac{2}{7} \times \frac{5}{7} \times \frac{2}{7} = \frac{100}{2401}$$

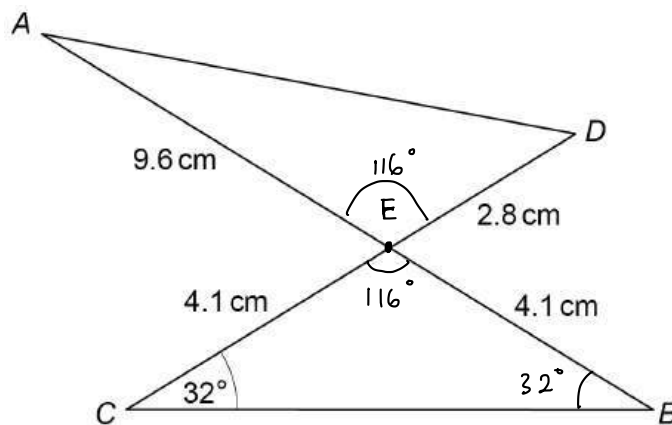
$$\frac{625}{2401} \div \frac{100}{2401} = 6.25$$

Answer

6.25



- 18 Lines AB , BC , CD and AD form two triangles.



Not drawn
accurately

Work out the length of AD .

[4 marks]

$$\hat{CBE} = 32^\circ$$

$$\hat{CEB} = 180 - 32 - 32 = 116^\circ$$

$$\hat{AED} = 116^\circ \text{ (vertically opposite angles are equal)}$$

$$AD^2 = 9.6^2 + 2.8^2 - 2(9.6)(2.8)\cos 116$$

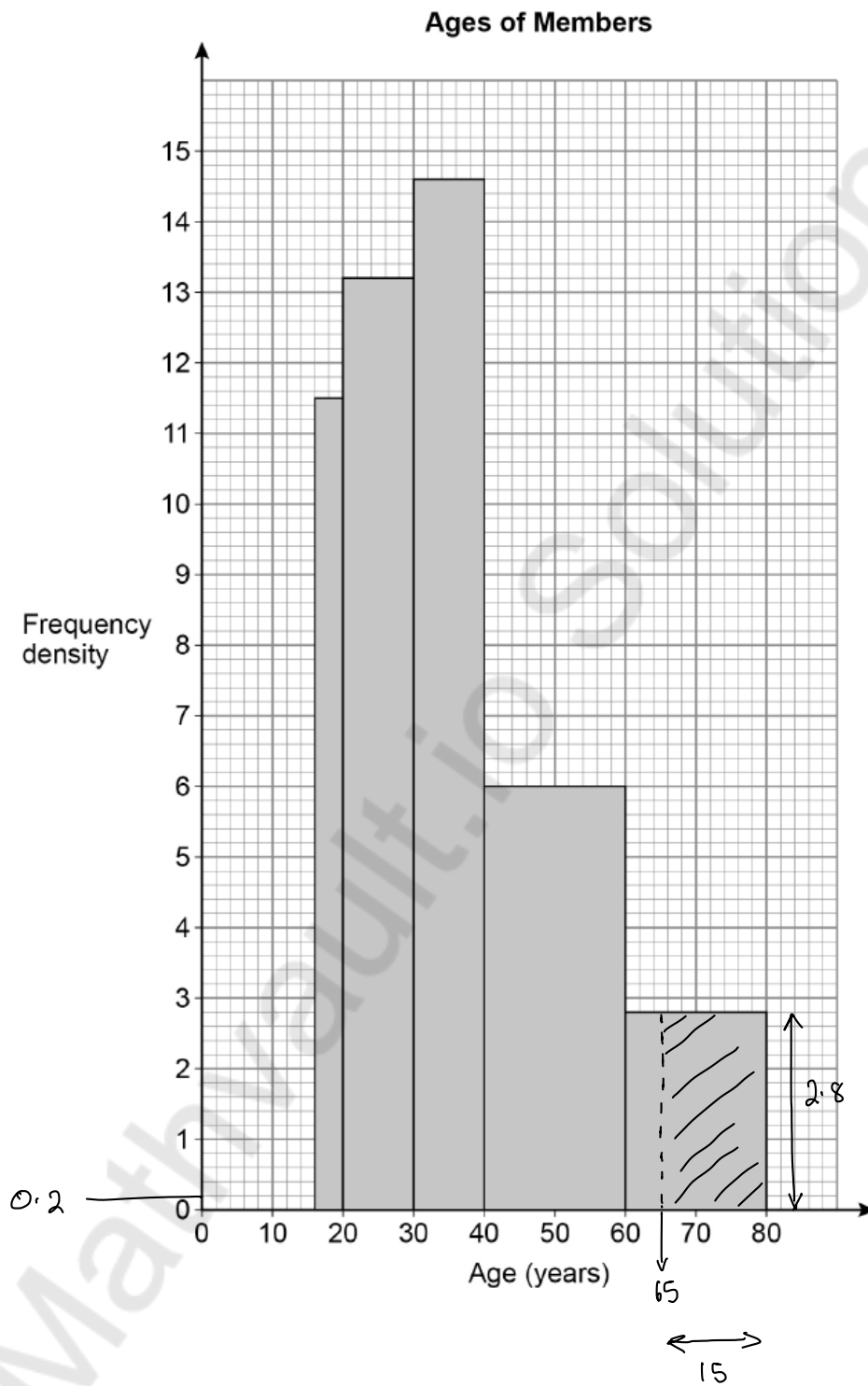
$$AD = \sqrt{9.6^2 + 2.8^2 - 2(9.6)(2.8)\cos 116}$$

Answer _____ | | • | _____ cm



19

The histogram represents the ages of the 500 members of a gym.
The first bar represents the members aged at least 16 and under 20



Each member pays an annual fee based on their age.

Age	Under 65	65 or over
Annual fee	£275	£129

Use the histogram to estimate the **total** annual fees paid by these members.

[4 marks]

$$\text{N}^{\circ} \text{ of } 65 \text{ or over} = 2.8 \times 15 = 42$$

$$\text{Fees from } 65 \text{ or over} = 42 \times 129 = \pounds 5418$$

$$\text{N}^{\circ} \text{ of under } 65 = 500 - 42 = 458$$

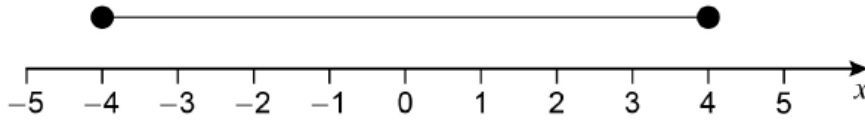
$$\text{Fees from under } 65 = 458 \times 275 = \pounds 125,950$$

$$\text{Total annual fees} = 125950 + 5418$$

$$\text{Answer } \pounds \underline{131,368}$$



- 20 David has solved the inequality $x^2 < 16$ and represented his solution on the number line below.



Give **one** reason why David's solution is wrong.

[1 mark]

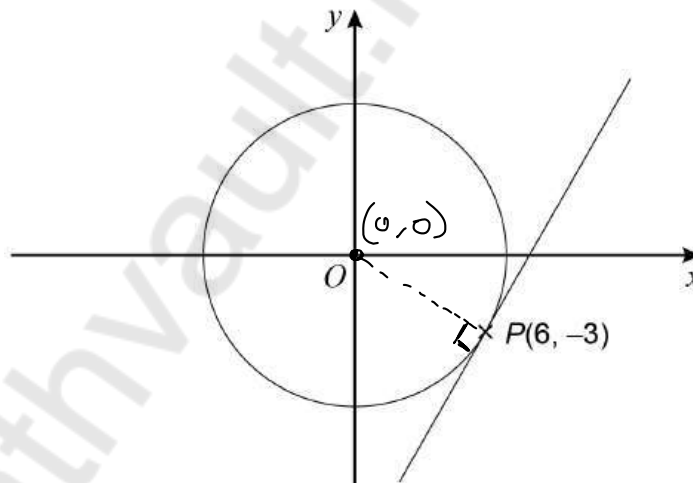
$$(-4)^2 = 16$$

$$16 \not< 16$$

$\therefore x = -4$ is not a solution

Circle at -4 and 4 should not be shaded

- 21 A circle with centre O and radius $\sqrt{45}$ has a tangent drawn at point $P(6, -3)$



Not drawn
accurately

- 21 (a) Write down the equation of the **circle**.

[1 mark]

Answer $x^2 + y^2 = 45$



21 (b) Work out the equation of the **tangent**.

Give your answer in the form $y = mx + c$

[4 marks]

$$m_r = \frac{-3-0}{6-0} = \frac{-3}{6} = -\frac{1}{2}$$

$$m_T = 2 \quad p(6, -3)$$

$$y = mx + c$$

$$y = 2x + c$$

$$-3 = 2(6) + c$$

$$-3 = 12 + c$$

$$\begin{array}{r} -12 \quad -12 \\ -15 = c \end{array}$$

$$\therefore y = 2x - 15$$

Answer $y = 2x - 15$

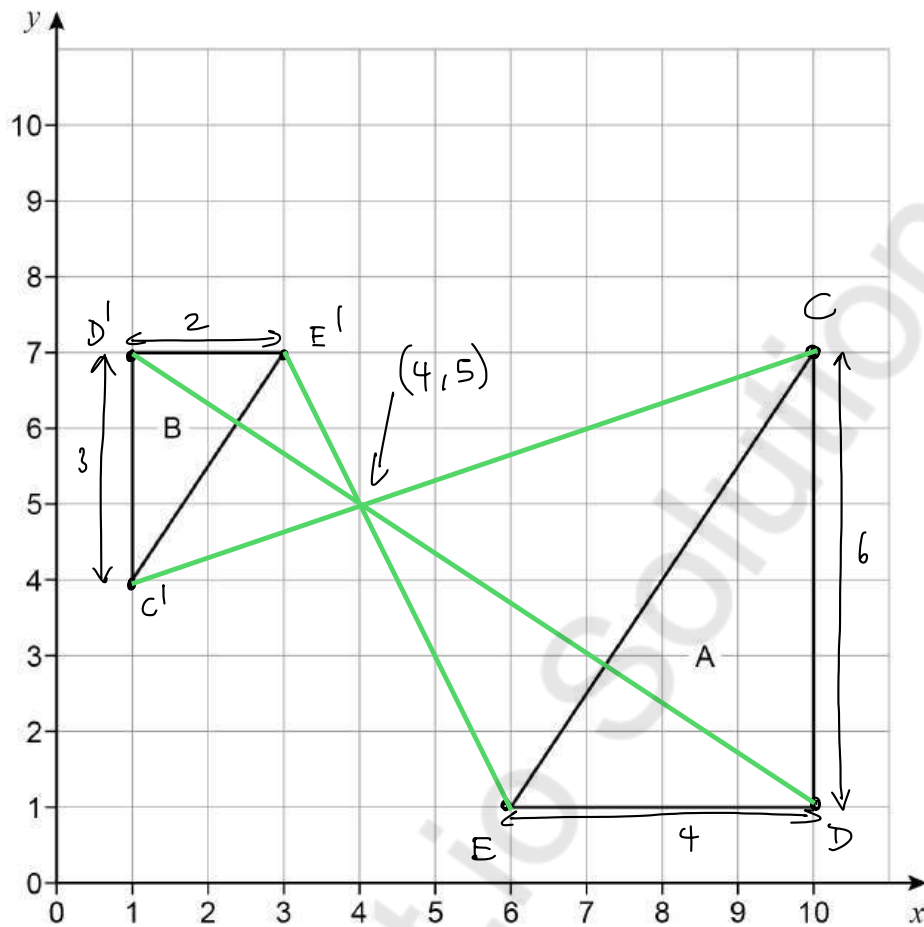
Turn over for the next question

Turn over ►



22

Shape A and shape B are shown on the grid.

Describe the **single** transformation that maps shape A to shape B.**[3 marks]**

Enlargement by a scale factor of $-\frac{1}{2}$
with a centre of enlargement at $(4, 5)$



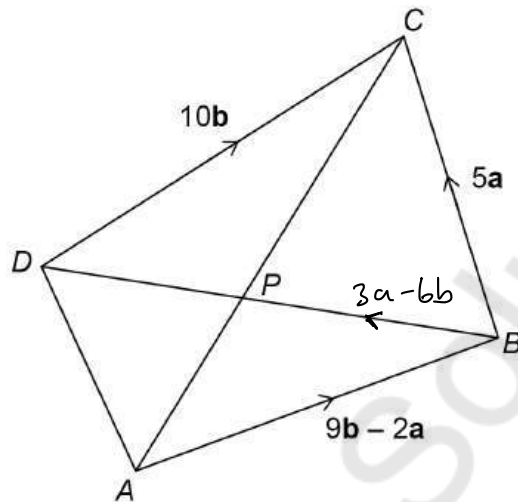
23

 $ABCD$ is a quadrilateral. AC and BD intersect at P .

$$\vec{AB} = 9\mathbf{b} - 2\mathbf{a}$$

$$\vec{BC} = 5\mathbf{a}$$

$$\vec{DC} = 10\mathbf{b}$$



$$BP : PD = 3 : 2$$

$$AP : PC = 1 : k$$

Work out the value of k .You **must** show your working.

[5 marks]

$$\vec{BD} = \vec{BC} + \vec{CD}$$

$$\vec{BD} = 5\mathbf{a} - 10\mathbf{b}$$

$$\vec{BP} = \frac{3}{5}\vec{BD} = \frac{3}{5}(5\mathbf{a} - 10\mathbf{b}) = 3\mathbf{a} - 6\mathbf{b}$$

$$\vec{PD} = \frac{2}{5}\vec{BD} = \frac{2}{5}(5\mathbf{a} - 10\mathbf{b}) = 2\mathbf{a} - 4\mathbf{b}$$

$$\vec{AP} = \vec{AB} + \vec{BP}$$

$$\vec{AP} = 9\mathbf{b} - 2\mathbf{a} + 3\mathbf{a} - 6\mathbf{b}$$

$$\vec{AP} = \mathbf{a} + 3\mathbf{b}$$

$$\vec{PC} = \vec{PB} + \vec{BC}$$

$$\vec{PC} = -\vec{BP} + \vec{BC}$$

$$\vec{PC} = -(3\mathbf{a} - 6\mathbf{b}) + 5\mathbf{a}$$

$$\vec{PC} = -3\mathbf{a} + 6\mathbf{b} + 5\mathbf{a}$$

$$\vec{PC} = 2\mathbf{a} + 6\mathbf{b}$$

$$\vec{PC} = 2\vec{AP}$$

$$\frac{1}{2} = \frac{\vec{AP}}{\vec{PC}}$$

$$1 : 2 = \vec{AP} : \vec{PC}$$

$$k = \underline{\quad 2 \quad}$$

Turn over ▶



- 24** A study suggests a student's exam mark, m , is directly proportional to the cube root of total revision time, t hours.
- A student doubles their total revision time.
- Work out the percentage increase in their exam mark.

[3 marks]

$$m \propto \sqrt[3]{t}$$

$$m = k \sqrt[3]{t}$$

$$m_1 = k \sqrt[3]{t}$$

$$m_2 = k \sqrt[3]{2t}$$

$$m_2 = k \times \sqrt[3]{2} \times \sqrt[3]{t}$$

$$m_2 = 1.26 k \sqrt[3]{t}$$

$$m_2 = 1.26 m_1$$

26% increase

Answer 26 %



25 $f(x) = ax + b$ and $g(x) = \frac{x+b}{a}$ where a and b are positive integers.

Prove that $fg(x) - af^{-1}(x)$ is always a multiple of 3

[4 marks]

$$fg(x) = f[g(x)] = a \left[\frac{x+b}{a} \right] + b$$

$$x+b+b$$

$$fg(x) = x+2b$$

$$x = ay + b$$

$$x - b = ay$$

$$\frac{x-b}{a} = y$$

$$f^{-1}(x) = \frac{x-b}{a}$$

$$af^{-1}(x) = a \times \frac{x-b}{a} = x-b$$

$$fg(x) - af^{-1}(x)$$

$$x+2b - (x-b)$$

$$x+2b - x + b$$

$$3b$$

$3b$ is always a multiple of 3

END OF QUESTIONS



There are no questions printed on this page

*Do not write
outside the
box*

**DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED**



