

Please write clearly in block capitals.

Centre number

Candidate number

Surname _____

Forename(s) _____

Candidate signature _____

I declare this is my own work.

GCSE MATHEMATICS

H

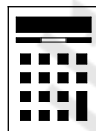
Higher Tier Paper 3 Calculator

Wednesday 11 June 2025 Morning Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

For Examiner's Use

Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
TOTAL	

Advice

In all calculations, show clearly how you work out your answer.



Answer **all** questions in the spaces provided.

1 Convert 8.25 pounds into kilograms.

Use 2.2 pounds = 1 kilogram

$$8.25 \text{ pounds} = x \text{ kilograms}$$

$$\begin{array}{r} 2.2 \times x \\ \hline \div 2.2 \end{array} = \begin{array}{r} 1 \times 8.25 \\ \hline \div 2.2 \end{array}$$

$$x = \frac{8.25}{2.2}$$

[2 marks]

Answer 3.75 kg

2 Here are the temperatures in six cities in degrees Celsius.

0°C -3°C 0°C 1.5°C 23°C 4°C

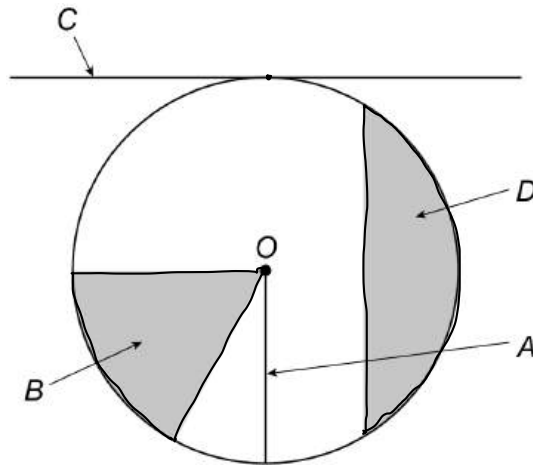
Write down the outlier.

[1 mark]

Answer 23 °C



3 Here is a circle, centre O



Match each letter to the correct word.

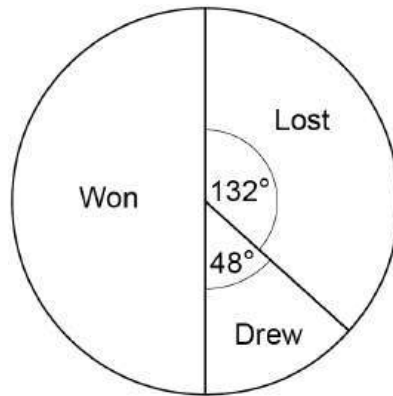
One has been done for you.

[3 marks]

	Arc
A	Chord
B	Diameter
C	Radius
D	Sector
	Segment
	Tangent



- 5 The pie chart represents the results of matches played by a team.



30 matches were **won**.

How many matches were lost?

[3 marks]

$$\text{Total matches} = 30 \times 2 = 60$$

$$\frac{11}{30} = \frac{132}{360} = \text{Fraction of lost games}$$

$$\frac{11}{30} \times 60 = 22 \text{ lost games}$$

Answer

22

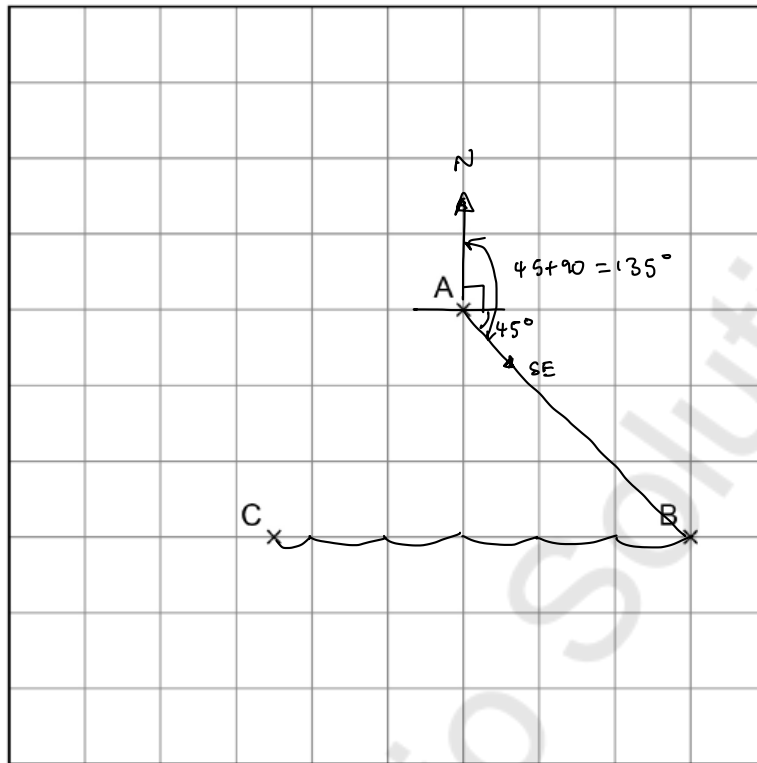
Turn over for the next question



- 6 Here is a scale diagram showing towns A, B and C on a centimetre grid.

1 cm : 200,000 cm

Scale 1 : 200 000



- 6 (a) Work out the **actual** distance from B to C.
Give your answer in kilometres.

[4 marks]

$$\begin{array}{l} \times 5.5 \left\{ \begin{array}{l} 5.5 \text{ cm} \\ 1 \text{ cm} \end{array} \right. \left\{ \begin{array}{l} 1,100,000 \text{ cm} \\ 200,000 \text{ cm} \end{array} \right. \left. \right\} \times 5.5 \end{array}$$

$$1 \text{ cm} = 1000 \text{ m}$$

$$1 \text{ m} = 100 \text{ cm}$$

$$1 \text{ km} = 100,000 \text{ cm}$$

$$11 \text{ km} = 1,100,000 \text{ cm}$$

$$\div 100,000$$

Answer 11 km



- 6 (b) B is South East of A.

Write down the bearing of B from A.

[1 mark]

Answer 135 °

- 7 (a) Write 2 weeks as a fraction of 8 days.

Give your answer in its simplest form.

[1 mark]

$$\begin{array}{l} \times 2 \left\{ \begin{array}{l} 1 \text{ week} = 7 \text{ days} \\ 2 \text{ weeks} = 14 \text{ days} \end{array} \right. \times 2 \end{array}$$

$$\frac{14}{8} \div 2 = \frac{7}{4}$$

Answer $\frac{7}{4}$

- 7 (b) Write 56 centimetres : 2.73 metres as a ratio in the form 1 : n

[1 mark]

$$\begin{array}{l} \downarrow \times 100 \\ 56 \text{ cm} : 273 \text{ cm} \\ \div 56 \left\{ \begin{array}{l} 1 \text{ cm} : \frac{39}{8} \text{ cm} \end{array} \right. \div 56 \end{array}$$

Answer 1 : $\frac{39}{8}$

7 (c) $A : B = \frac{1}{5} : \frac{7}{10}$

Write A as a fraction of B.

[2 marks]

$$A : B$$

$$\frac{1}{5} : \frac{7}{10}$$

$$\begin{array}{cc} \times 10 & \times 10 \\ 2 : 7 \end{array}$$

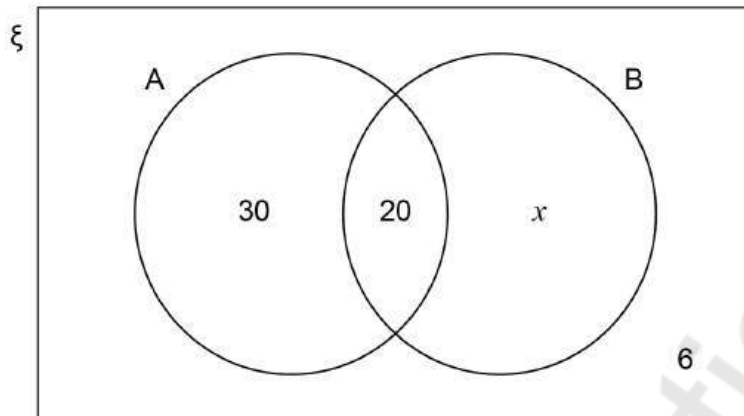
$$2 : 7$$

$$A : B$$

Answer $\frac{2}{7}$



- 10 The Venn diagram shows some of the **numbers** of items in each set.



$$P(A) = \frac{1}{2}$$

Work out the value of x .

[2 marks]

$$\text{half of all items are in } A = 30 + 20 = 50$$

$$\text{Total items} = 100$$

$$100 = 30 + 20 + x + 6$$

$$100 - 30 - 20 - 6 = x$$

$$x = 44$$

$$x = \underline{\quad 44 \quad}$$

Turn over for the next question

Turn over ►



11 (a) Write down the equation of a straight line parallel to $y - 2x = 9$ [1 mark]
 $y = mx + c$ $+2x + 2x$

$$y = 2x + 9$$

$$m = 2$$

Answer $y = 2x + 1$

11 (b) A straight line

- has gradient 5
- passes through the point (3, 7)

Circle the equation of the line.

[1 mark]

$$y = 3x - 2$$

$$y = 3x + 7$$

~~$$y = 5x$$~~

$$y = 5x - 8$$

$$15 \neq 7$$

$$y = 15$$

$$y = 5 \times 3$$

$$y = 5 \times 3 - 8$$

$$y = 15 - 8$$

$$y = 7$$



12 Rob records the time he takes to drive to work every day for 80 days. The table shows information about the results.

Midpoint	Time, t (minutes)	Frequency	Midpoint	fx
$\frac{20+25}{2}$	$20 \leq t < 25$	16	22.5	$16 \times 22.5 = 360$
$\frac{25+30}{2}$	$25 \leq t < 30$	32	27.5	$32 \times 27.5 = 880$
$\frac{30+40}{2}$	$30 \leq t < 40$	24	35	$24 \times 35 = 840$
$\frac{40+60}{2}$	$40 \leq t < 60$	8	50	$8 \times 50 = 400$
	Total = 80			<u>2480</u>

Last year, the **mean** time Rob took to drive to work was 25 minutes.

Estimate the percentage increase in the **mean** driving time for these 80 days.

[4 marks]

Estimated Mean = $\frac{2480}{80} = 31$ minutes

$\frac{31 - 25}{25} \times 100 = 24\%$

Answer 24 %



- 13** The table shows information about the salary of 90 employees.

Salary, s (£)	Frequency
$0 < s \leq 20\,000$	44
$20\,000 < s \leq 40\,000$	22
$40\,000 < s \leq 60\,000$	14
$60\,000 < s \leq 80\,000$	5
$80\,000 < s \leq 100\,000$	2
$100\,000 < s \leq 120\,000$	3

- 13 (a)** Complete the cumulative frequency table.

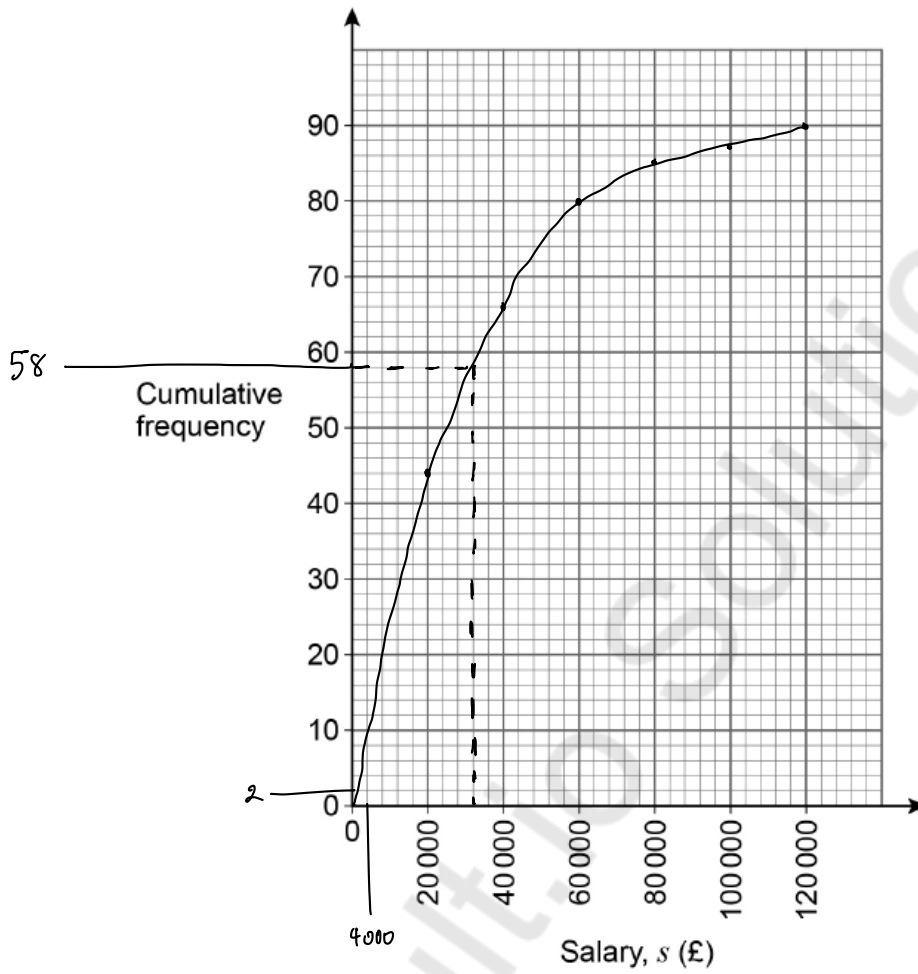
[1 mark]

Salary, s (£)	Cumulative Frequency
$s \leq 20\,000$	44
$s \leq 40\,000$	66
$s \leq 60\,000$	80
$s \leq 80\,000$	85
$s \leq 100\,000$	87
$s \leq 120\,000$	90



13 (b) Draw a cumulative frequency diagram to represent the data.

[2 marks]



13 (c) Estimate the number of employees with a salary **less** than £32 000

[2 marks]

Answer 58

5

Turn over ►



14 (a) For a small plane,

- the mass of the empty plane is 800 kg, to the nearest 100 kg
- the mass of fuel is 190 kg, to the nearest 5 kg
- the mass of the passengers is 163 kg, to the nearest kg

The total mass of a plane is calculated by adding these three masses.

The **maximum** mass for the plane to take off safely is 1200 kg

Can this plane definitely take off safely?

Tick a box.

Yes

No

Show working to support your answer.

[4 marks]

$$\begin{array}{ccccccc}
 700 & \vdots & 800 & \vdots & 900 & 185 & \vdots & 190 & \vdots & 195 \\
 | & & | & & & | & & | & & | \\
 750 \leq EP < 850 & & & & & 187.5 \leq F < 192.5 & & & & \\
 \hline
 & & & & & 162 & \vdots & 163 & \vdots & 164 \\
 & & & & & & & & & \\
 & & & & & 162.5 \leq P < 163.5 & & & &
 \end{array}$$

$$\text{Max possible mass} \leq 850 + 192.5 + 163.5$$

$$\text{Max possible mass} < 1206$$

but $1206 > 1200$ Thus it is possible that the mass is a safety risk.

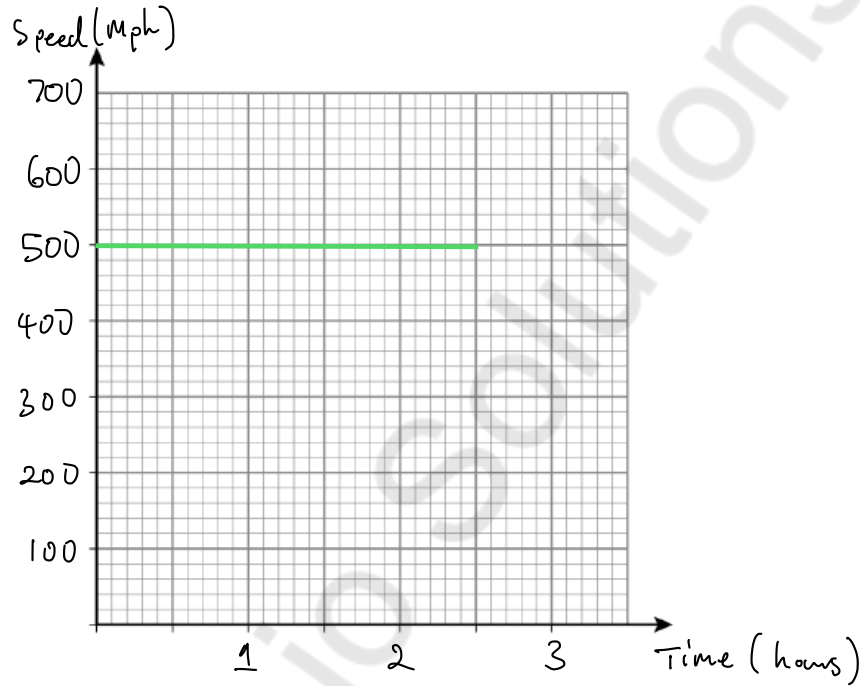


- 14 (b)** A different plane travels 1250 miles in 2 hours 30 minutes at a constant speed.

On the grid, draw a **speed/time** graph to represent this information.

[3 marks]

$$\text{Speed} = \frac{1250}{2.5} = 500 \text{ miles/hour}$$



Turn over for the next question

Turn over ►



15

Amy and Becky each make integers using **three** single digits.

In any integer, digits may be repeated.

- Amy makes **even** integers with a first digit greater than 7
- Becky makes **odd** integers with a first digit that is non-zero.

They each make as many different integers as possible.

How many **more** integers than Amy does Becky make?

[3 marks]

$$\begin{array}{l}
 8, 9 \text{] Greater than 7 but still single digits} \\
 \square \square \square \quad 5 \text{ even integers} \\
 \text{N}^\circ \text{ of possible numbers for Amy} = 2 \times 10 \times 5 = 100 \\
 \hline
 1, 2, 3, 4, 5, 6, 7, 8, 9 \text{] Possibilities for first digit.} \\
 \square \square \square \quad \text{N}^\circ \text{ of possible numbers for Becky} = 9 \times 10 \times 5 = 450 \\
 \hline
 450 - 100 = 350
 \end{array}$$

Answer 350



16

 x is a **positive even number**.

$$y = (x - 3)(x - 5)(x + 6)$$

Without expanding brackets,

explain why there is only one value of x for which y is **negative**.**[3 marks]**

$$\text{let } x = 2$$

$$y = (2-3)(2-5)(2+6)$$

$$y = -1 \times -3 \times 8 = 24$$

$$\text{let } x = 4$$

$$y = (4-3)(4-5)(4+6)$$

$$y = 1 \times -1 \times 10 = -10$$

$$\text{let } x = 6$$

$$y = (6-3)(6-5)(6+6)$$

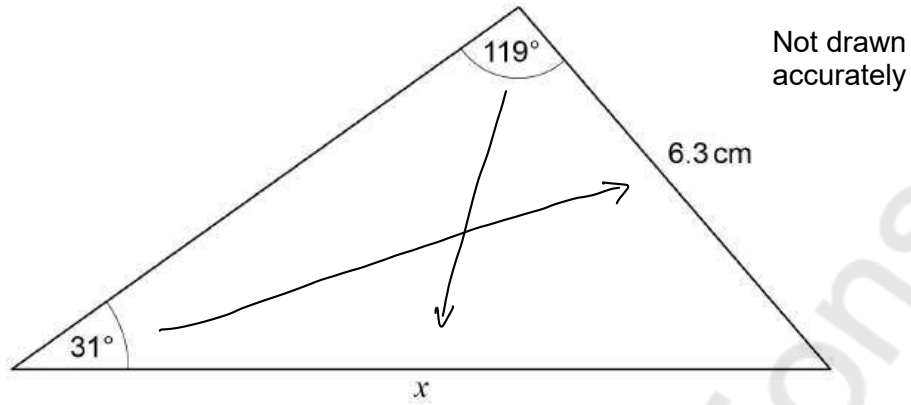
$$y = 3 \times 1 \times 12 = 36$$

Turn over for the next question

Turn over ►



17

Use the sine rule to work out x .**[2 marks]**

$$\frac{\sin 31}{6.3} = \frac{\sin 119}{x}$$

$$x \sin 31 = 6.3 \sin 119$$

$$x = \frac{6.3 \sin 119}{\sin 31}$$

$$x = 10.7 \text{ cm (3 s.f.)}$$

$$x = 10.7 \text{ cm}$$



18

Here are the first four terms of a quadratic sequence.

6 15 28 45

Work out an expression for the n th term.**[3 marks]**

$ \begin{array}{ccccccc} 6 & & 15 & & 28 & & 45 \\ & \curvearrowright & & \curvearrowright & & \curvearrowright & \\ & +9 & & +13 & & +17 & \\ & & \curvearrowright & & \curvearrowright & & \\ & & +4 & & +4 & & \\ & \nearrow & & & & & \\ 2a & & & & & & \end{array} $	$an^2 + bn + c$ $2n^2 + bn + c$ <p>At $n=1$ $2(1)^2 + b(1) + c = 6$</p> $2 + b + c = 6$ $b + c = 4$ <p>At $n=2$ $2(2)^2 + b(2) + c = 15$</p> $8 + 2b + c = 15$ $2b + c = 7$ $- \quad \underline{b + c = 4}$ $\quad \quad \quad \underline{\quad} = 3$ $3 + c = 4$ $c = 1$
$2a = 4$ $a = 2$	

Answer $2n^2 + 3n + 1$

Turn over for the next question

Turn over ►



19 On the grid, identify the region represented by

$$x + y < 5 \quad \text{and} \quad y < 2x + 4 \quad \text{and} \quad y \geq 1$$

$$y = 5$$

$$\text{At } x = 1$$

$$y = -1 + 5$$

$$y = 4$$

Label the region R.

$$y < -x + 5$$

$$(0, 5)$$

$$(1, 4)$$

$$(1, 6)$$

$$(0, 4)$$

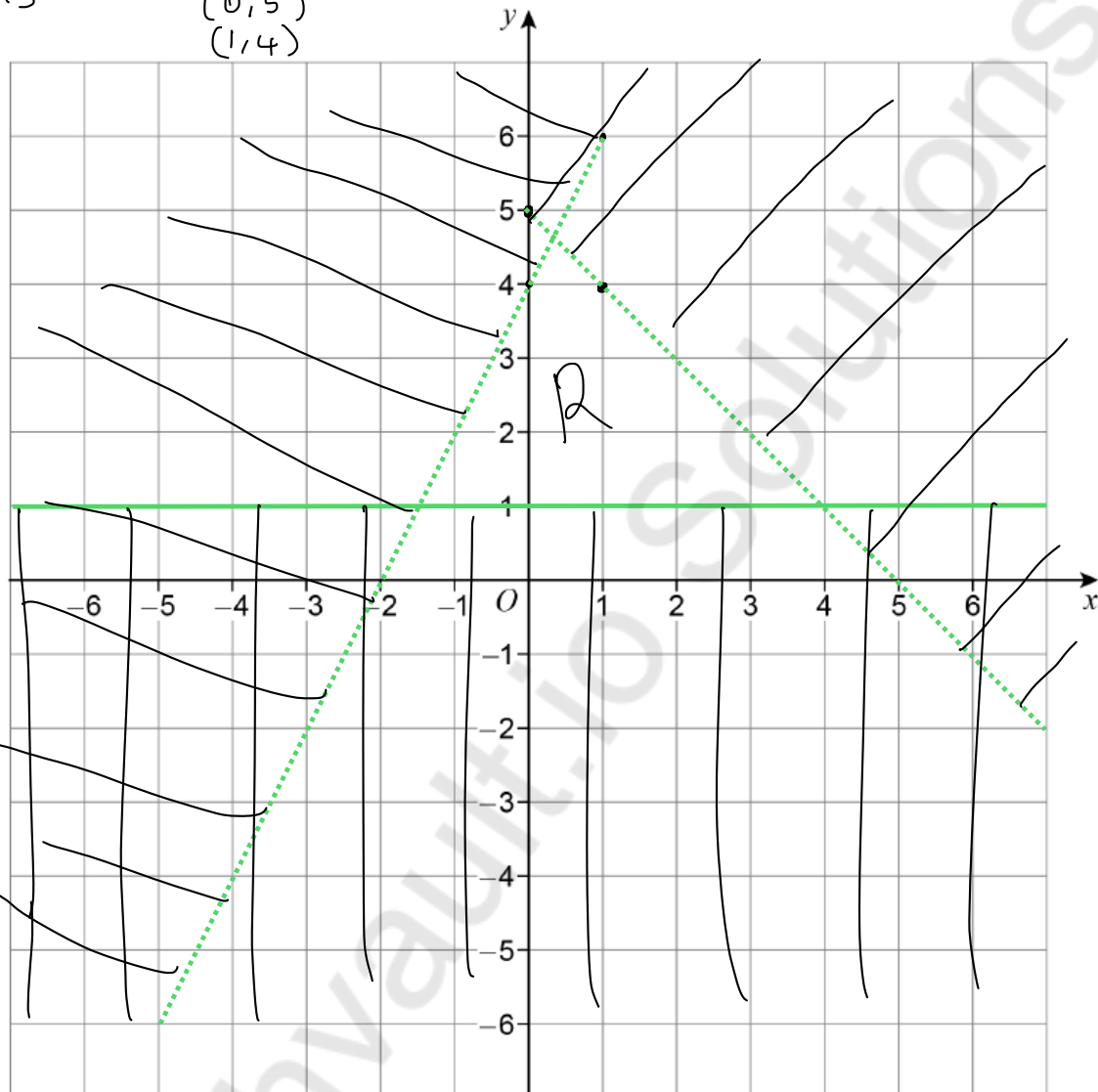
$$\text{At } x = 1$$

$$y = 2(1) + 4 = 6$$

$$\text{At } x = 0$$

$$y = 2(0) + 4 = 4$$

[4 marks]



20 (a) Factorise fully $3n^2 + 5n + 2$

$$3 \times 2 = \frac{6}{3, 2}$$

[2 marks]

$$3n^2 + 3n + 2n + 2$$

$$3n(n+1) + 2(n+1)$$

$$(3n+2)(n+1)$$

Answer $(3n+2)(n+1)$

20 (b) A sequence has n th term $3n^2 + 5n + 2$

Are any of the terms in the sequence a prime number?

Tick a box.

Yes

No

Give a reason for your answer.

[1 mark]

$3n^2$ is never a prime number

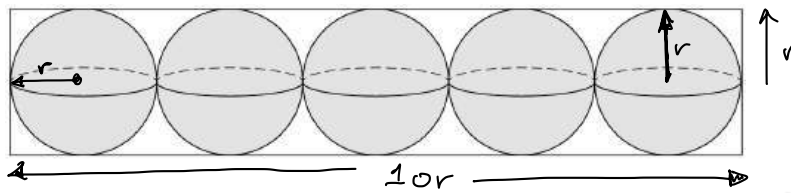
$5n$ is never a prime number

Turn over for the next question

Turn over ►



21

Five identical spheres just fit inside a **cylinder**.Each sphere has radius r .

$$\text{Volume of a sphere} = \frac{4}{3}\pi r^3$$

What fraction of the space inside the **cylinder** is filled by the spheres?You **must** show your working.**[4 marks]**

$$\text{Volume of cylinder} = \pi r^2 h = \pi r^2 (10r) = 10\pi r^3$$

$$\text{Volume of 5 spheres} = 5 \times \frac{4}{3}\pi r^3 = \frac{20}{3}\pi r^3$$

$$\frac{\frac{20}{3}\pi r^3}{10\pi r^3} = \frac{20}{3} \times \frac{1}{10} = \frac{2}{3}$$

Answer $\frac{2}{3}$



22

$$\text{Solve } 2x^2 > 12 - 5x$$

$$\begin{array}{r} -12 \\ -12 \end{array}$$

$$2x - 12 = -24$$

[4 marks]

$$\begin{array}{r} 2x^2 - 12 > -5x \\ + 5x \quad + 5x \end{array}$$

$$\begin{array}{r} 24, -1 \\ 12, -2 \\ 8, -3 \end{array}$$

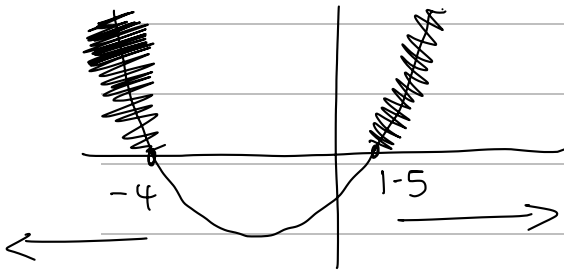
$$2x^2 + 5x - 12 > 0$$

$$2x^2 + 8x - 3x - 12 > 0$$

$$2x(x+4) - 3(x+4) > 0$$

$$(2x-3)(x+4) > 0$$

$$\text{Critical Values: } x = \frac{3}{2} \quad x = -4$$



$$\text{Answer } x < -4 \quad x > 1.5$$

Turn over for the next question

Turn over ►



23

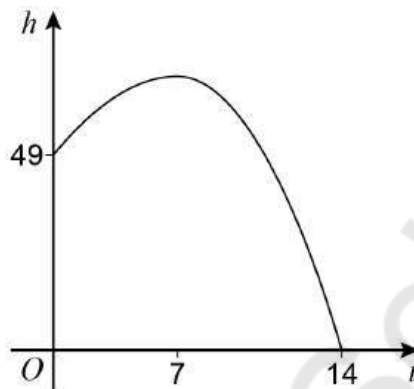
A roller coaster starts at ground level.

The height above ground level, h , in metres, of the roller coaster is given by

$$h = -(t - 7)^2 + 49$$

where t is the time in seconds after the roller coaster starts.

Sam draws a graph of h against t for $0 \leq t \leq 14$



$$\begin{aligned} h &= -(0 - 7)^2 + 49 \\ h &= -49 + 49 \\ h &= 0 \end{aligned}$$

Make **two** criticisms of Sam's graph.

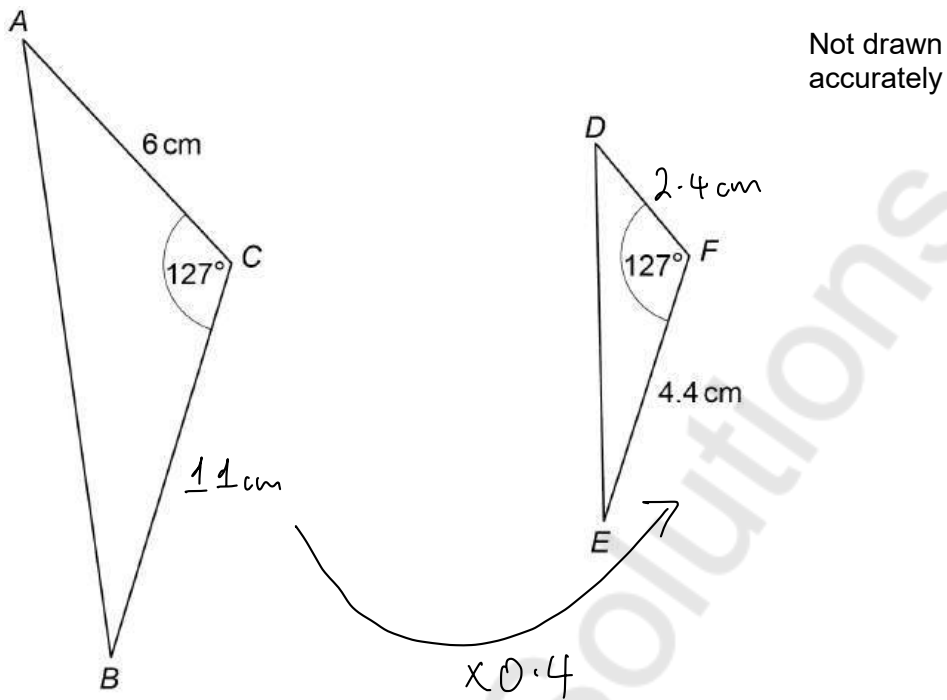
[2 marks]

Criticism 1 y-intercept is incorrect it should be
(0, 0)

Criticism 2 The turning point is incorrect. It
should be (7, 49)



24

Triangles ABC and DEF are similar.The area of ABC is 26.355 cm^2 Work out the area of DEF .**[4 marks]**

$$26.355 = \frac{1}{2} \times 6 \times BC \times \sin 127$$

$$2 \times 26.355 = 6 BC \sin 127$$

$$\frac{2 \times 26.355}{6 \sin 127} = BC$$

$$11 \text{ cm} = BC$$

$$DF = 6 \times 0.4 = 2.4 \text{ cm}$$

$$\text{Area of } \triangle DEF = \frac{1}{2} \times 4.4 \times 2.4 \times \sin 127 \approx 4.22 \text{ cm}^2 \text{ (3sf)}$$

Answer 4.22 cm²**END OF QUESTIONS**

There are no questions printed on this page

*Do not write
outside the
box*

**DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED**

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