

Answer ALL questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

- 1 The table shows information about the times, in minutes, 100 people took to complete a bike race.

Midpoint

$$\frac{120+140}{2} = 130$$

150

170

190

210

Time (t minutes)	Frequency
$120 \leq t < 140$	12
$140 \leq t < 160$	28
$160 \leq t < 180$	30
$180 \leq t < 200$	22
$200 \leq t < 220$	8

On the grid below, draw a frequency polygon for this information.

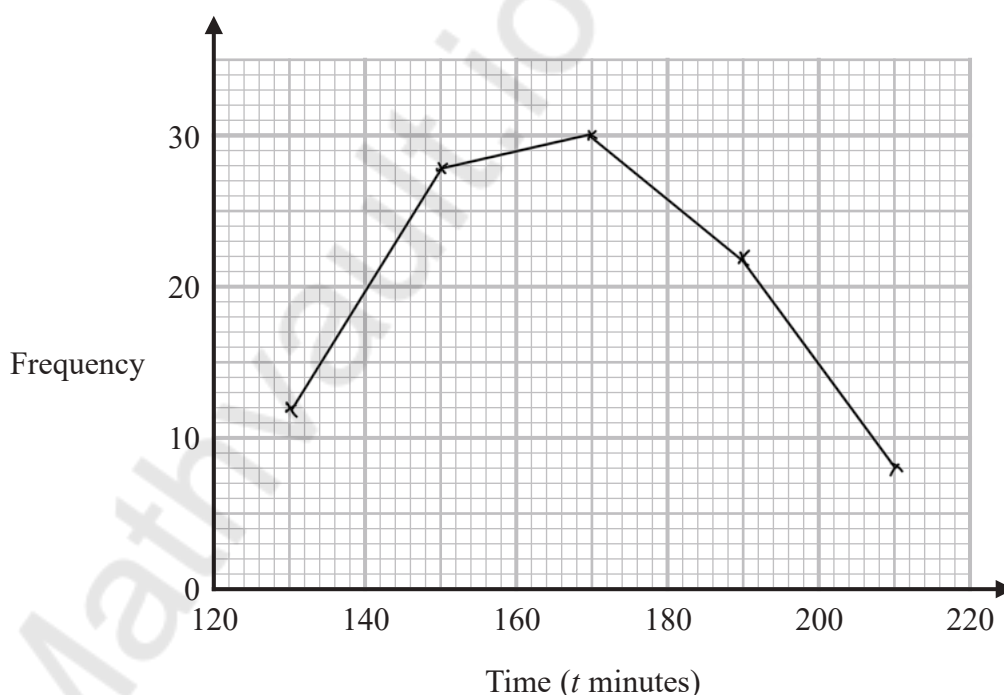
130, 12

150, 28

170, 30

190, 22

210, 8



(Total for Question 1 is 2 marks)



- 2 (a) Write 3.402×10^5 as an ordinary number.

3 4 0 2 0 0

340,200

(1)

- (b) Write 0.8026 in standard form.

$$\frac{0.8026 \times 10}{10}$$

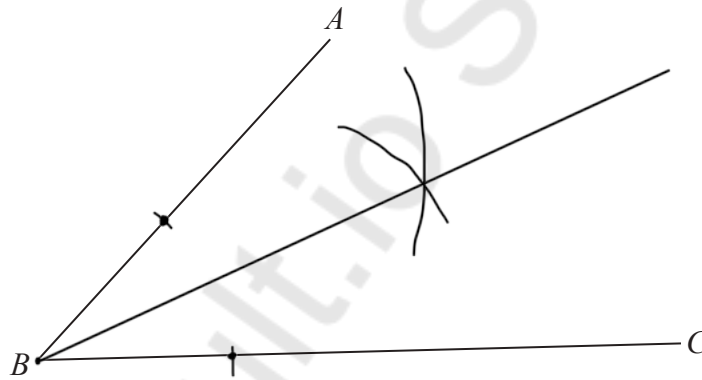
$$8.026 \times 10^{-1}$$

$$8.026 \times 10^{-1}$$

(1)

(Total for Question 2 is 2 marks)

- 3 Use ruler and compasses to construct the bisector of angle ABC .
You must show your construction lines.



(Total for Question 3 is 2 marks)

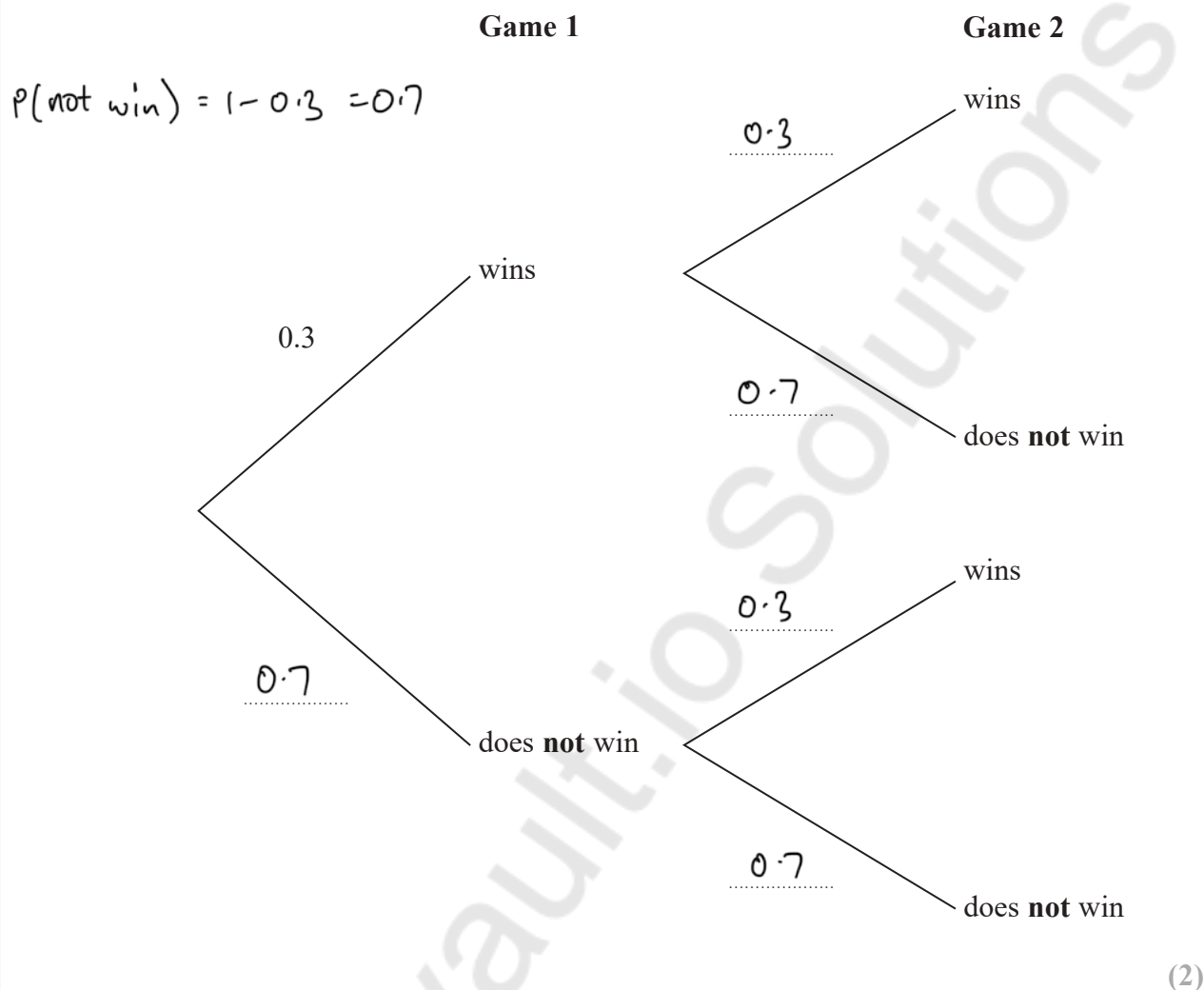


4 Dan is playing cards.

The probability that he will win a game of cards is 0.3

Dan plays two games of cards.

(a) Complete the probability tree diagram.



(b) Work out the probability that Dan does **not** win either game.

$$p(\text{Neither game win}) = 0.7 \times 0.7$$

$$0.49$$

(2)

(Total for Question 4 is 4 marks)



5 Robyn buys a total of 240 pens and pencils, where

$$\text{number of pens : number of pencils} = \frac{3}{5}$$

Robyn pays 9p for each pen.
She sells each pen for 11p.

$$\frac{240}{8} = 30$$

Robyn pays 6p for each pencil.
She sells each pencil for 10p.

$$\text{Number of Pens} = 3 \times 30 = 90$$

$$\text{Number of Pencils} = 5 \times 30 = 150$$

Robyn sells all of the pens and pencils.

Work out Robyn's percentage profit.
Give your answer correct to 1 decimal place.
You must show all your working.

$$9 \times 90 = 810 \text{ p} - \text{buying}$$

$$11 \times 90 = 990 \text{ p} - \text{selling}$$

$$6 \times 150 = 900 \text{ p} - \text{buying}$$

$$10 \times 150 = 1500 \text{ p} - \text{selling}$$

$$\text{Total buying Cost} = 810 + 900 = 1710 \text{ p}$$

$$\text{Total Selling revenue} = 990 + 1500 = 2490 \text{ p}$$

$$\% \text{ profit} = \frac{2490 - 1710}{1710} \times 100 = \underline{\underline{45.6\%}}$$

45.6 %

(Total for Question 5 is 5 marks)



P 7 5 1 6 2 A 0 5 2 4

6 The stem and leaf diagram shows the test scores of 23 students from School A.

3	0
4	1 2 4 4 5 7
5	3 4 4 6 7 8 8 8
6	0 1 1 1 1
7	1 1 2

Key:

3 | 0 represents 30

23 students from School B did the same test.

Their median score was 56

The range of their scores was 47

Compare the distribution of the test scores of the students from School A with the distribution of the test scores of the students from School B.

Median of School A = 57

Range of School A = $79 - 30 = 49$

The median of School A is higher than the median of School B.

The range of School A is higher than the range of School B.

(Total for Question 6 is 4 marks)



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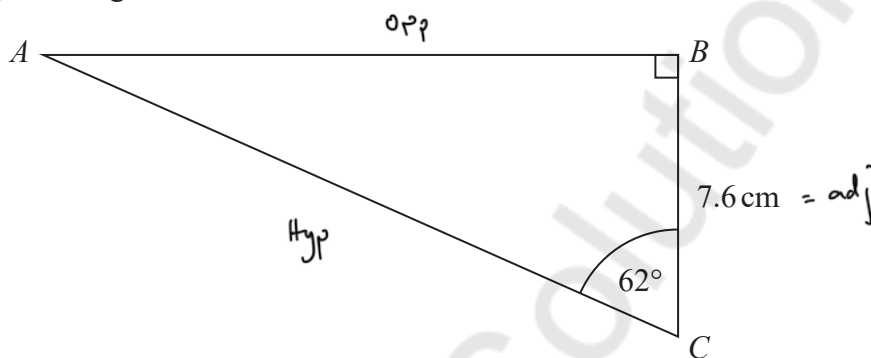
- 7 Jana used her calculator to find the value of a number t .
The answer on her calculator began 10.2

Complete the error interval for t .

$$\underline{10.2} \dots \leq t < \dots \underline{10.3}$$

(Total for Question 7 is 2 marks)

- 8 ABC is a right-angled triangle.



Calculate the length of AB .

Give your answer correct to 1 decimal place.

$$\tan 62 = \frac{AB}{7.6}$$

$$AB = 7.6 \times \tan 62$$

$$\dots \underline{14.3} \dots \text{ cm}$$

(Total for Question 8 is 2 marks)



9 (a) Simplify fully $2x^3y^5 \times 7x^2y^1$

$$14x^{3+2} \times y^{5+1}$$

$$\underline{14a^5y^6} \quad (2)$$

(b) Simplify $(m^2)^{-3}$

$$m^{2 \times -3}$$

$$\underline{m^{-6}}$$

(1)

(Total for Question 9 is 3 marks)

10 In a sale, the normal prices are reduced by 15%
Amina buys a dress in the sale for £46.75

Work out the normal price of the dress.

$$\begin{aligned}
 100\% & \Rightarrow x \\
 \downarrow -15\% \\
 85\% & \Rightarrow £46.75 \\
 \div 85 & \\
 1\% & \Rightarrow £0.55 \\
 \times 100 & \\
 100\% & \Rightarrow £55
 \end{aligned}$$

$$£ \quad \underline{55.00}$$

(Total for Question 10 is 2 marks)

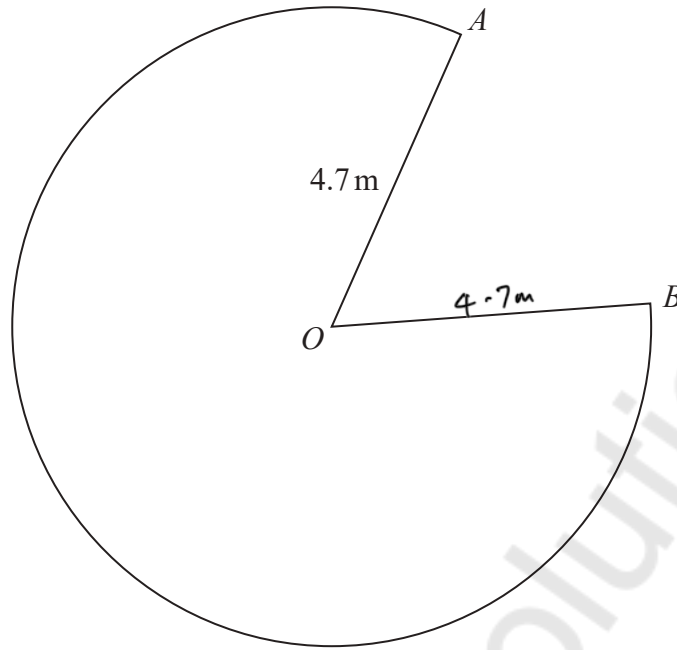


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11 OAB is a sector of a circle with centre O and radius 4.7 m.



The sector has a perimeter of 34.3 m.

Find the size of the reflex angle AOB .

Give your answer correct to the nearest degree.

$$\widehat{AB} = 34.3 - 4.7 - 4.7$$

$$\widehat{AB} = 24.9 \text{ m}$$

$$\frac{\theta}{360} \times 2\pi r = \text{Length of arc}$$

$$\frac{\theta}{360} \times 2\pi \times 4.7 = 24.9$$

$$\theta = \frac{24.9 \times 360}{2\pi \times 4.7}$$

304

(Total for Question 11 is 3 marks)



P 7 5 1 6 2 A 0 9 2 4

12 Rudi invests £4500 in a savings account.

He gets compound interest at a rate of

2.4% for the first year $\Rightarrow \times 1.024$

1.8% for each extra year. $\Rightarrow \times 1.018$

(a) Work out the value of Rudi's investment at the end of 3 years.

$$4500 \times 1.024 \times 1.018^2$$

$$\pounds \underline{4775.38}$$

(3)

Bruna buys a car for £7500

The value of the car depreciates by $x\%$ each year.

At the end of 2 years the value of the car is £4107

(b) Work out the value of x .

$$7500 \times (1 - x)^2 = 4107$$

$$(1 - x)^2 = \frac{4107}{7500}$$

$$1 - 2x + x^2 = 0.5476$$

$$x^2 - 2x + 0.4524 = 0$$

$$x^2 - 2x + \frac{1131}{2500} = 0$$

$$2500x^2 - 5000x + 1131 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-5000) \pm \sqrt{(-5000)^2 - 4(2500)(1131)}}{2(2500)}$$

$$x = 1.74 \quad x = \underline{\underline{0.26}}$$

reject
due to
depreciation

$$x = \underline{\underline{26\%}}$$

(3)

(Total for Question 12 is 6 marks)

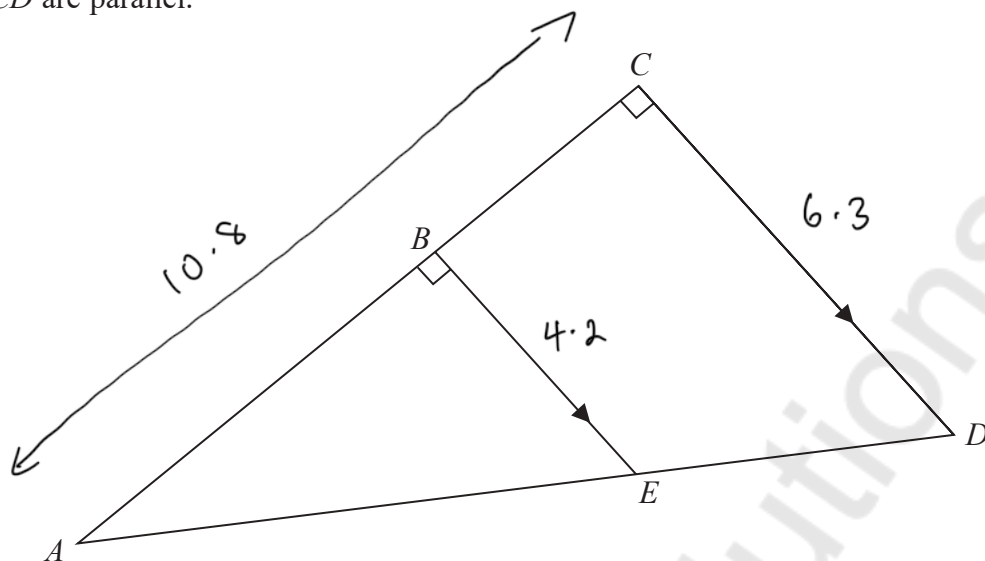


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- 13 ABC and AED are straight lines.
 BE and CD are parallel.



$$BE = 4.2 \text{ cm}$$

$$CD = 6.3 \text{ cm}$$

$$AC = 10.8 \text{ cm}$$

Work out the area of trapezium $BCDE$.

$$\text{Area of big triangle} = \frac{b \times h}{2} = \frac{10.8 \times 6.3}{2} = 34.02$$

$$S_T : b_T = 4.2 : 6.3$$

$$S_T : 10.8$$

$$S_T = \frac{4.2 \times 10.8}{6.3}$$

$$S_T = 7.2$$

$$\text{Area of small triangle} = \frac{4.2 \times 7.2}{2} = 15.12$$

$$\text{Area of trapezium} = 34.02 - 15.12$$

18.9

..... cm²

(Total for Question 13 is 3 marks)



P 7 5 1 6 2 A 0 1 1 2 4

14 Prove algebraically that $0.4\dot{6}\dot{2}$ can be written as $\frac{229}{495}$

$$0.4\dot{6}\dot{2} = 0.462\dot{6}\dot{2} = x$$

$$1000x = 462.\dot{6}\dot{2}$$

$$10x = 4.\dot{6}\dot{2}$$

$$1000x - 10x = 458$$

$$990x = 458$$

$$x = \frac{458}{990} = \frac{229}{495}$$

(Total for Question 14 is 3 marks)

15 Make p the subject of the formula $t = \frac{2(2p-3)}{5-2p}$

$$t(5-2p) = 4p-6$$

$$5t - 2pt = 4p - 6$$

$$5t + 6 = 4p + 2pt$$

$$5t + 6 = p(4 + 2t)$$

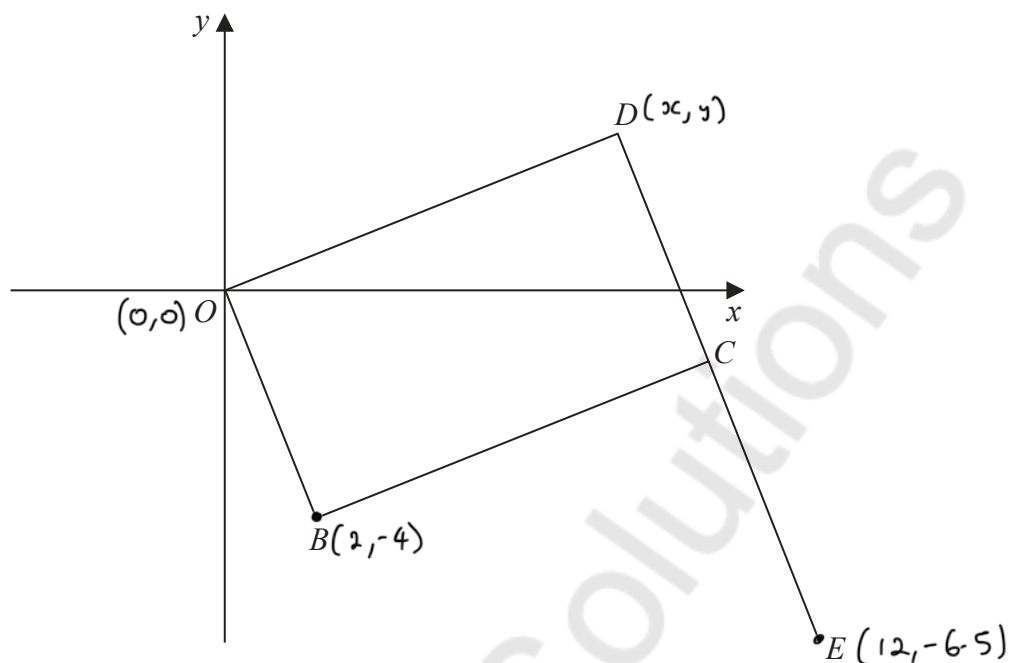
$$p = \frac{5t + 6}{4 + 2t}$$

$$p = \frac{5t + 6}{4 + 2t}$$

(Total for Question 15 is 4 marks)



- 16 $OBCD$ is a rectangle.
 DCE is a straight line.



B has coordinates $(2, -4)$

E has coordinates $(12, -6.5)$

Work out the coordinates of D .

You must show all your working.

$$M_{OB} = \frac{-4 - 0}{2 - 0} = -2$$

$$M_{DE} = -2 \quad OB \text{ and } DE \text{ are parallel}$$

$$y - (-6.5) = -2(x - 12)$$

$$y + 6.5 = -2x + 24$$

$$y = -2x + 17.5 \quad (\text{line } DE)$$

$$M_{OB} = \frac{-1}{M_{OD}}$$

$$M_{OD} = \frac{-1}{M_{OB}}$$

$$M_{OD} = \frac{1}{2}$$

$$y - 0 = \frac{1}{2}(x - 0)$$

$$y = \frac{1}{2}x \quad (\text{line } OD)$$

Equate OD to DE

$$\frac{1}{2}x = -2x + 17.5$$

$$2.5x = 17.5$$

$$x = 7$$

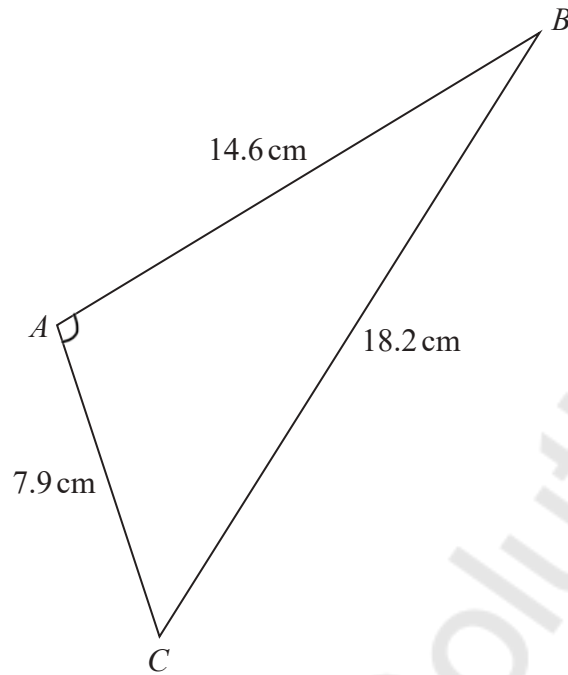
$$y = \frac{7}{2}$$

(..... 7, $\frac{7}{2}$ )

(Total for Question 16 is 5 marks)



17 Here is triangle ABC .



Work out the area of triangle ABC .

Give your answer correct to 3 significant figures.

$$18.2^2 = 7.9^2 + 14.6^2 - 2(7.9)(14.6)\cos A$$

$$\cos A = \frac{7.9^2 + 14.6^2 - 18.2^2}{2(7.9)(14.6)}$$

$$A = \cos^{-1}\left(\frac{-5567}{23068}\right)$$

$$A \approx 103.965^\circ \dots$$

$$\text{Area} = \frac{1}{2}ab\sin C$$

$$A_T = \frac{1}{2} \times 7.9 \times 14.6 \times \sin 103.965^\circ$$



..... 56.0 cm^2

(Total for Question 17 is 4 marks)



18 Maria wants to find an estimate for the number of frogs in a lake.

On Saturday she catches 40 of the frogs.
She puts a tag on each frog and releases them.

On Monday she catches 55 of the frogs.
11 of the frogs have tags.

- (a) Work out an estimate for the total number of frogs in the lake.
You must show all your working.

40 total tags

$$\frac{11}{55} \text{ with tags} \qquad \frac{40}{x}$$

$$\frac{11 \div 11}{55 \div 11} = \frac{1 \times 40}{5 \times 40} = \frac{40}{200}$$

200

(3)

- (b) State one assumption you have made.

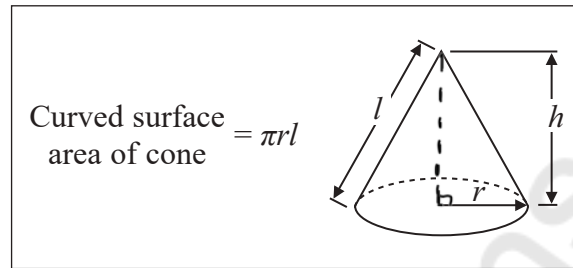
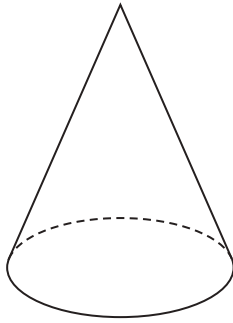
We have assumed the total number of frogs on Saturday and Monday are the same.

(1)

(Total for Question 18 is 4 marks)



19 The diagram shows a cone.



The radius of the base of the cone is $\frac{3}{4}$ of the height of the cone.

The total surface area of the cone is $54\pi \text{ cm}^2$

Work out the height of the cone.

$$r = \frac{3}{4}h$$

$$\pi r l + \pi r^2 = 54\pi$$

$$r l + r^2 = 54$$

$$\frac{3}{4} h l + \left(\frac{3}{4} h\right)^2 = 54$$

$$\frac{3}{4} h \left(\frac{5}{4} h\right) + \frac{9}{16} h^2 = 54$$

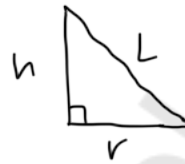
$$\frac{15}{16} h^2 + \frac{9}{16} h^2 = 54$$

$$24 h^2 = 16 \times 54$$

$$h^2 = \frac{16 \times 54}{24}$$

$$h^2 = 36$$

$$h = \sqrt{36}$$



$$L^2 = r^2 + h^2$$

$$L^2 = \left(\frac{3}{4}h\right)^2 + h^2$$

$$L^2 = \frac{9}{16}h^2 + h^2$$

$$L^2 = \frac{25}{16}h^2$$

$$L = \frac{5}{4}h$$

6

..... cm

(Total for Question 19 is 4 marks)



20 Solve the simultaneous equations

$$\begin{aligned}y^2 &= 3x^2 + 4 \\ y + 2x &= 7\end{aligned}$$

Give your solutions correct to 3 significant figures.

$$y = 7 - 2x$$

$$(7 - 2x)^2 = 3x^2 + 4$$

$$49 - 28x + 4x^2 = 3x^2 + 4$$

$$45 - 28x + x^2 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-28) \pm \sqrt{(-28)^2 - 4(1)(45)}}{2(1)}$$

$$x \approx 26.3$$

$$x \approx 1.71$$

$$y = 7 - 2(26.3), \quad y \approx -45.6$$

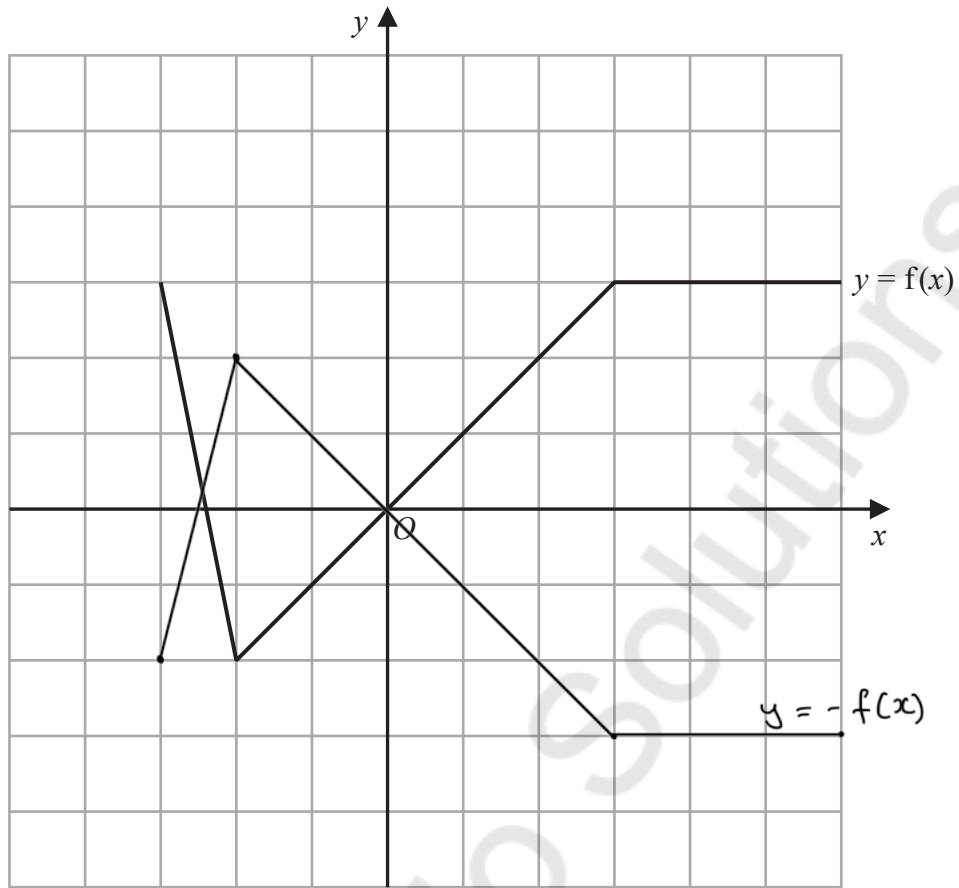
$$y = 7 - 2(1.71), \quad y \approx 3.57$$

$$x \approx 26.3 \quad y \approx -45.6 \quad x \approx 1.71 \quad y \approx 3.57$$

(Total for Question 20 is 4 marks)



21 Here is the graph of $y = f(x)$



(a) On the grid, draw the graph of $y = -f(x)$

(1)

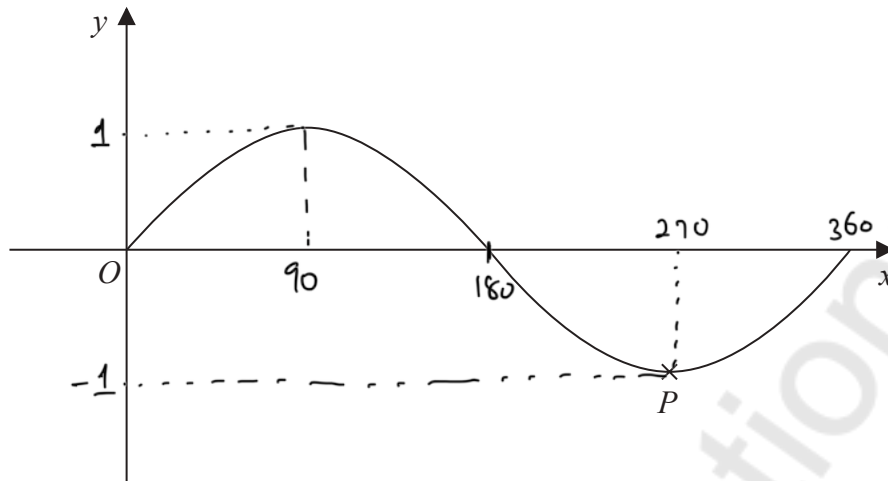
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Here is a sketch of the graph of $y = \sin x^\circ$



The point marked P is a turning point on the graph.

The graph of $y = \sin x^\circ$ is translated to give the graph of $y = \sin(x + 180)^\circ + 4$

Following the translation the point P , shown on the graph above, moves to point R .

(b) Find the coordinates of R .

$$270 - 180 = 90$$

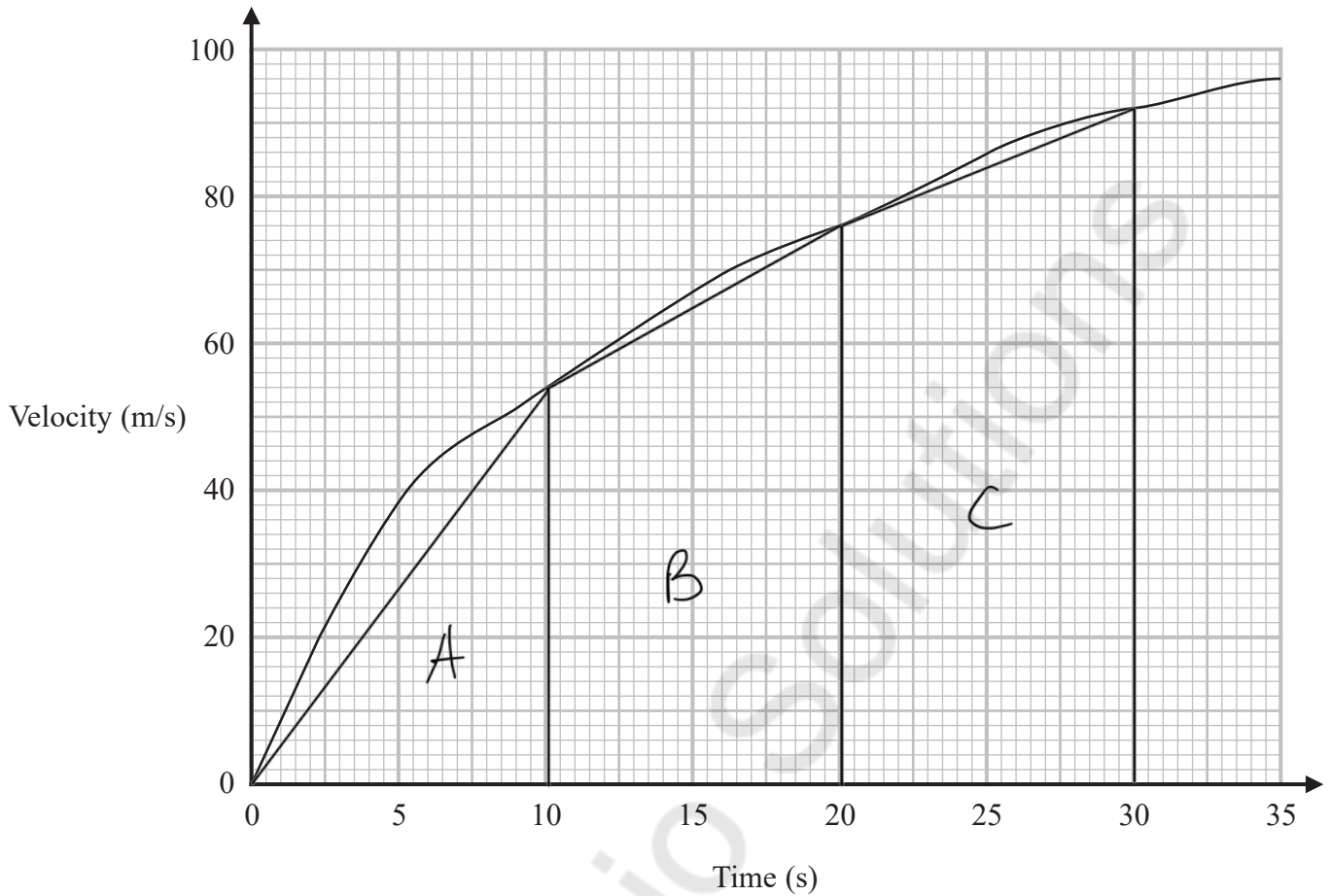
$$-1 + 4 = 3$$

$$\left(\underline{90}, \underline{3} \right)$$

(Total for Question 21 is 4 marks)



22 Here is a velocity-time graph for an aeroplane.



Work out an estimate for the distance the aeroplane travelled in the first 30 seconds.
Use 3 strips of equal width.

$$A: \frac{10 \times 54}{2} = 270 \text{ m}$$

$$B: \frac{(54 + 76) \times 10}{2} = 650 \text{ m}$$

$$C: \frac{(76 + 92) \times 10}{2} = 840 \text{ m}$$

$$\begin{array}{l} \text{Estimated} \\ \text{Total} \\ \text{distance} \end{array} = 270 + 650 + 840$$

1760 m

(Total for Question 22 is 3 marks)



23 Sketch the graph of

$$y = x^2 - 6px - 7 \quad \text{where } p > 0$$

showing the coordinates of the turning point, in terms of p , and the coordinates of the intercept with the y -axis.

You must show all your working.

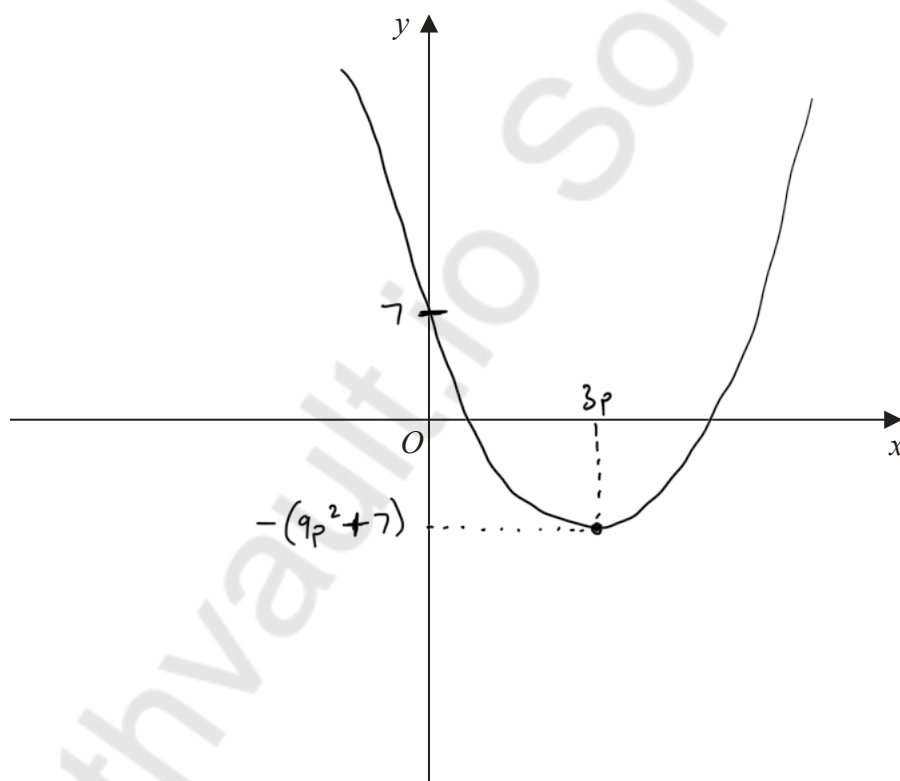
$$y\text{-intercept} : (0, 7)$$

$$\text{Turning Point} : (3p, -9p^2 - 7)$$

$$y = x^2 - 6px - 7$$

$$y = (x - 3p)^2 - 9p^2 - 7$$

$$y = (x - 3p)^2 + (-9p^2 - 7)$$



(Total for Question 23 is 5 marks)

TOTAL FOR PAPER IS 80 MARKS



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