

GCSE (9–1) Mathematics

J560/01 Paper 1 (Foundation Tier)

Tuesday 6 November 2018 – Morning

Time allowed: 1 hour 30 minutes



You may use:

- a scientific or graphical calculator
- geometrical instruments
- tracing paper



First name										
Last name										
Centre number						Candidate number				

INSTRUCTIONS

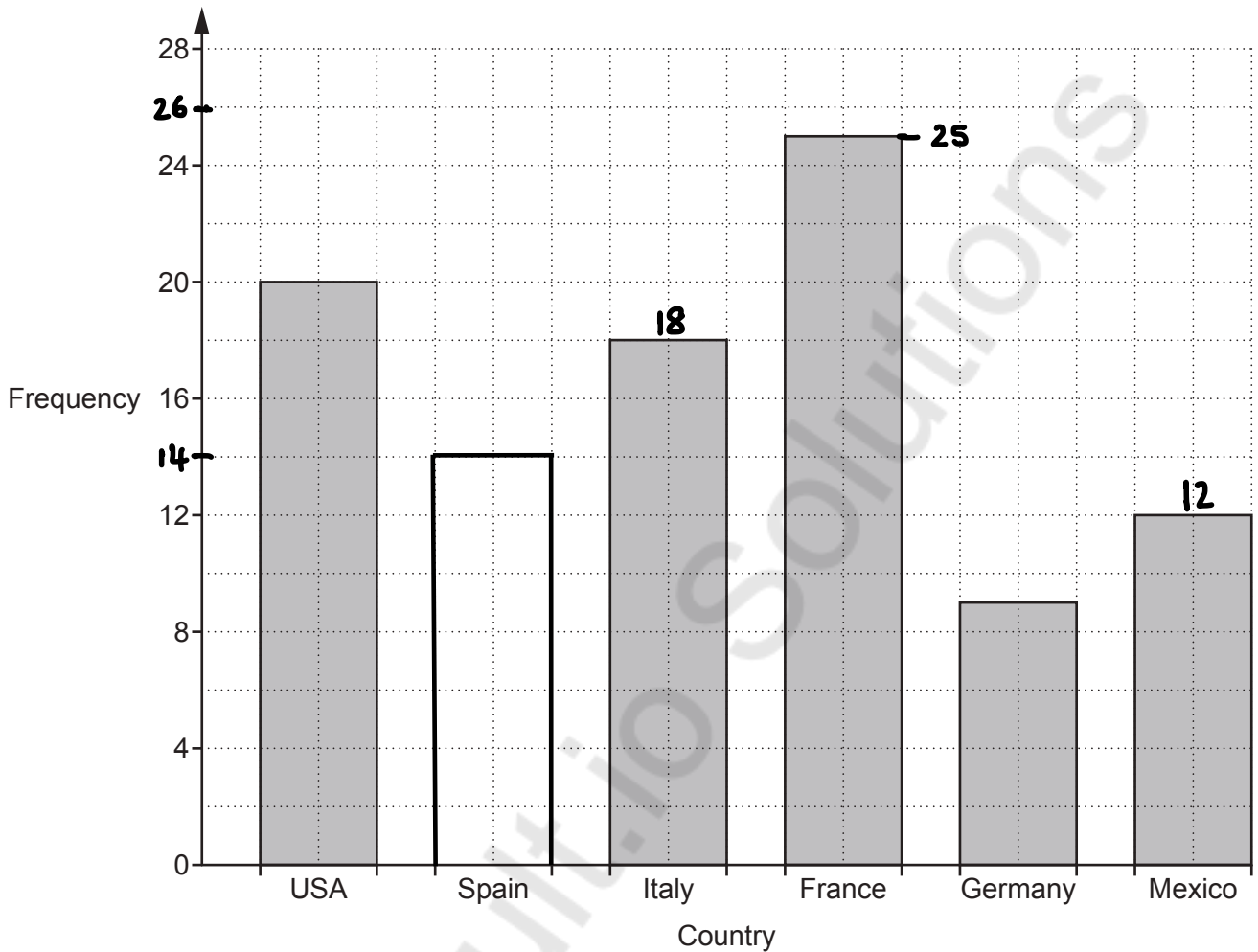
- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number and candidate number.
- Answer **all** the questions.
- Read each question carefully before you start to write your answer.
- Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided. If additional space is required, use the lined page(s) at the end of this booklet. The question number(s) must be clearly shown.
- Do **not** write in the barcodes.

INFORMATION

- The total mark for this paper is **100**.
- The marks for each question are shown in brackets [].
- Use the π button on your calculator or take π to be 3.142 unless the question says otherwise.
- This document consists of **20** pages.

Answer **all** the questions.

- 1 Jodie asked some people to choose from six countries where they would most like to go on holiday. The bar chart shows her results for five of the countries.



- (a) 14 people answered Spain.

Show this information on the bar chart.

[1]

- (b) Complete these sentences.

(i) **Germany** was chosen by the fewest people.

[1]

(ii) **25** people chose France.

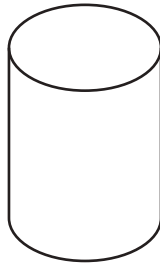
[1]

(iii) **6** **more** people chose Italy than Mexico.

[1]

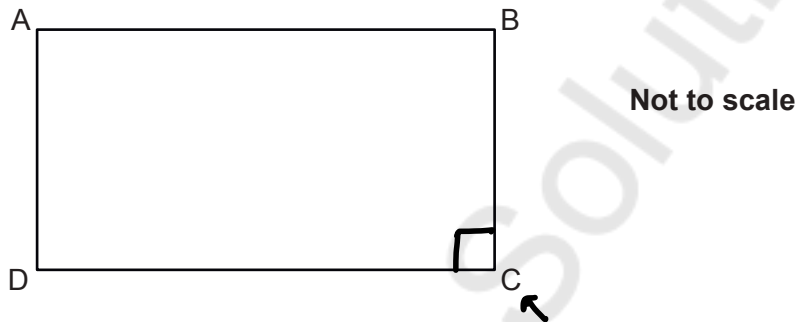
$$18 - 12$$

- 2 (a) Write down the mathematical name of this solid.



(a) *Cylinder* [1]

- (b) ABCD is a rectangle.



Add the correct mathematical symbol to the diagram to show that angle BCD is a right angle. [1]

- 3 Louiza changes £320 into euros.
£1 is worth 1.14 euros.

x1.14
How many euros does she receive?

$$320 \times 1.14 = 364.8$$

..... *364.80* euros [2]

4 (a) Write down each of the following.

(i) An even number.

(a)(i) **2** [1]

(ii) A factor of 25.

1 25
5

(ii) **5** [1]

(iii) A prime number between 10 and 20.

11, 13, 17, 19

(iii) **11** [1]

(iv) A cube number.

$$2^3 = 2 \times 2 \times 2 = 8$$

(iv) **8** [1]

(b) Find the highest common factor (HCF) of 35 and 91.

35	91
1 35	1 91
5 7	7 13

(b) **7** [2]

- 5 (a) Write 3 : 57 as a ratio in its simplest form.

$$\begin{array}{r} 3 : 57 \\ \div 3 \quad \div 3 \\ 1 : 19 \end{array}$$

(a) **1** : **19** [1]

- (b) Bob and Chris share some money in the ratio 2 : 3.
Bob receives £8.

Work out how much Chris receives.

$$\begin{array}{r} B : C \\ 2 : 3 \\ \times 4 \quad \times 4 \\ \pounds 8 : \pounds 12 \end{array}$$

(b) £ **12** [2]

- 6 Solve.

(a) $x - 6 = 4$
 $+6 \quad +6$
 $x = 10$

(a) $x =$ **10** [1]

(b) $\frac{12}{x} = 3$

$$\frac{12}{4} = 3$$

(b) $x =$ **4** [1]

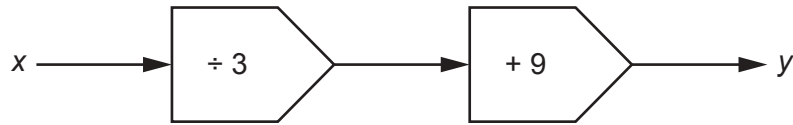
- 7 (a) Round 81.4**6**9 to 1 decimal place.

(a) **81.5** [1]

- (b) Round 0.005**6**94 to 3 significant figures.

(b) **0.00569** [1]

- 8 Here is a function.
The input is x and the output is y .



Write an algebraic expression for y in terms x .

$$\frac{x}{3} + 9 = y$$

$$y = \frac{x}{3} + 9 \dots\dots\dots [2]$$

- 9 Liu wants to decorate some cakes with shapes.

She has 140 shapes.

Each shape is a star or a heart.

The ratio of the number of stars : number of hearts is 4 : 3.

She wants to put 5 stars and 4 hearts on each cake.

How many cakes can Liu decorate?

Show full working to support your answer.

$$S : H$$

$$4 : 3 \quad \text{Total 7 parts}$$

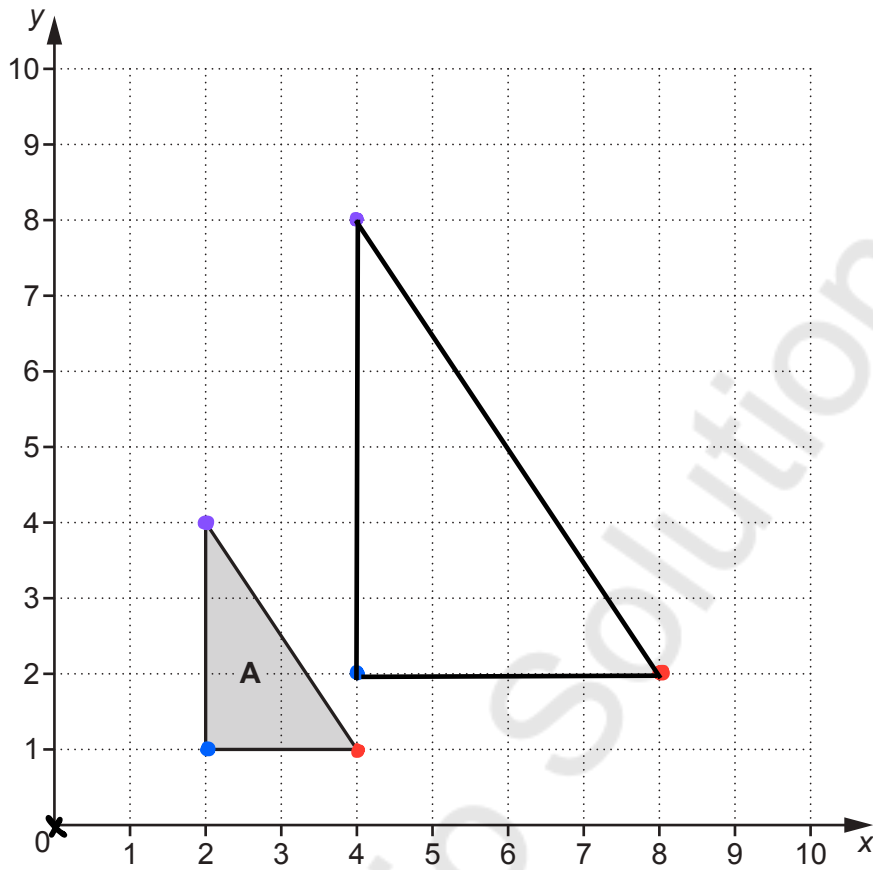
$$140 \div 7 = 20$$

$$\times 20 \quad \times 20$$

$$\text{Stars} = 80 \quad \div 5 = 16 \text{ cakes}$$

$$\text{Heart} = 60 \quad \div 4 = 15 \text{ cakes}$$

10 Triangle **A** is drawn on the grid below.



$$\begin{pmatrix} 2 \\ 1 \end{pmatrix} \times 2 = \begin{pmatrix} 4 \\ 2 \end{pmatrix}$$

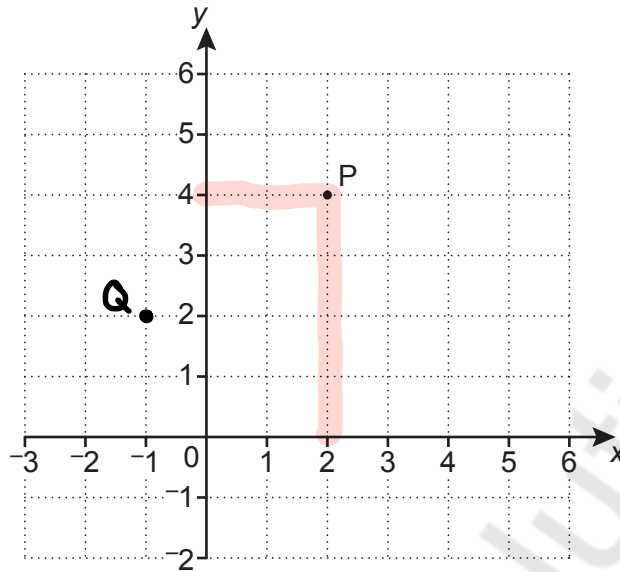
$$\begin{pmatrix} 4 \\ 1 \end{pmatrix} \times 2 = \begin{pmatrix} 8 \\ 2 \end{pmatrix}$$

$$\begin{pmatrix} 2 \\ 4 \end{pmatrix} \times 2 = \begin{pmatrix} 4 \\ 8 \end{pmatrix}$$

Enlarge triangle **A** with scale factor 2 and centre of enlargement (0, 0).

[3]

11 Point P is shown on this grid.



(a) Write down the coordinates of point P.

(a) (.....**2**.....,**4**.....) [1]

(b) Plot point Q at (-1, 2).

[1]

12 Use the formula

$$v = u + at$$

to find the final velocity, when

- the initial velocity is 8 m/s - **u**
- the acceleration is 3 m/s² - **a**
- the time is 5 seconds. - **t**

$$\begin{aligned} v &= 8 + 3 \times 5 \\ &= 8 + 15 \\ &= 23 \end{aligned}$$

.....**23**..... m/s [2]

13 Calculate the circumference of a circle with diameter 10 cm.

$$\begin{aligned} C &= \pi d \\ &= \pi(10) \\ &= 31.415\dots \\ &\approx 31.4 \end{aligned}$$

..... 31.4 cm [2]

14 (a) Find the value of x in each of the following.

(i) $a^4 \times a^3 = a^x$

$$4 + 3$$

(a)(i) $x = \dots 7 \dots$ [1]

(ii) $(b^4)^3 = b^x$

$$4 \times 3$$

(ii) $x = \dots 12 \dots$ [1]

(b) Factorise fully.

$$18x^2 + 9x$$

$$\text{HCF of } 18 \text{ and } 9 = 9$$

$$\text{HCF of } x^2 \text{ and } x = x$$

$$18x^2 + 9x$$

$$9x(2x + 1)$$

(b) $9x(2x + 1)$ [2]

15 Tea bags of similar quality are sold in three different sized packs:

Small Pack
80 tea bags for £2.10

Medium pack
150 tea bags for £3.55

Large pack
220 tea bags for £5.25

- (a) Which pack is the best value for money?
Show how you decide.

Small pack

$$£2.10 \div 80 = 0.02625 \text{ for 1 tea bag}$$

Medium pack

$$£3.55 \div 150 = 0.0236 \text{ for 1 tea bag}$$

Large Pack

$$£5.25 \div 220 = 0.023863 \text{ for 1 tea bag}$$

.....Medium..... because $0.0236 < 0.02625$ and 0.02363

..... [4]

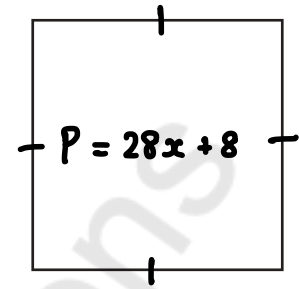
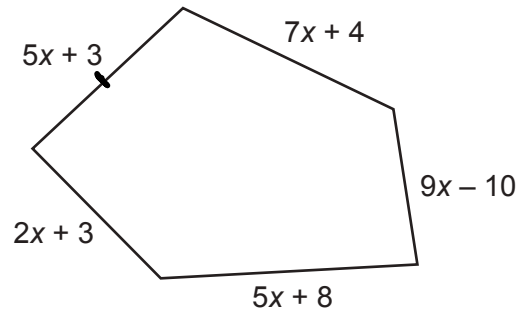
- (b) Explain why someone may buy a pack which is not the best value for money.

.....They have not done this calculation.....

..... [1]

- 16 The perimeter of the pentagon is equal to the perimeter of the square.

Not to scale



Find an expression for the length of one side of the square.
Give your answer in terms of x in its simplest form.

Perimeter of Pentagon

$$= 5x + 3 + 7x + 4 + 9x - 10 + 5x + 8 + 2x + 3$$

$$= 28x + 8$$

One side length

$$\frac{28x + 8}{4} = 7x + 2$$

..... $7x + 2$ [4]

- 17 James works from 2pm until 8.30pm on both Thursday and Friday. He is paid £12 per hour.

On Saturday he is paid $1\frac{1}{2}$ times this hourly pay.

He works for 5 hours on Saturday.

Calculate how much James earns **in total** for these three days.

Thursday & Friday

$$2\text{pm} - 8.30\text{pm} = 6.5 \text{ hours}$$

$$£12 \times 6.5 = £78$$

$$£78 \times 2 = £156$$

Saturday

$$1.5 \times 12 = £18 \text{ per hour}$$

$$5 \times 18 = £90$$

Total earnings

$$= £156 + £90$$

$$= £246$$

£ 246 [6]

- 18 Doctor Jones starts an appointment every 20 minutes. Doctor Warholm starts an appointment every 35 minutes.

The first appointment for both doctors starts at 8.30 am.

What is the next time that they have an appointment start at the same time?

Dr. Jones 20 40 60 80 100 120 **140** 160 ...

Dr Warholm 35 70 105 **140** 175

$$\text{LCM} = 140 \text{ mins}$$

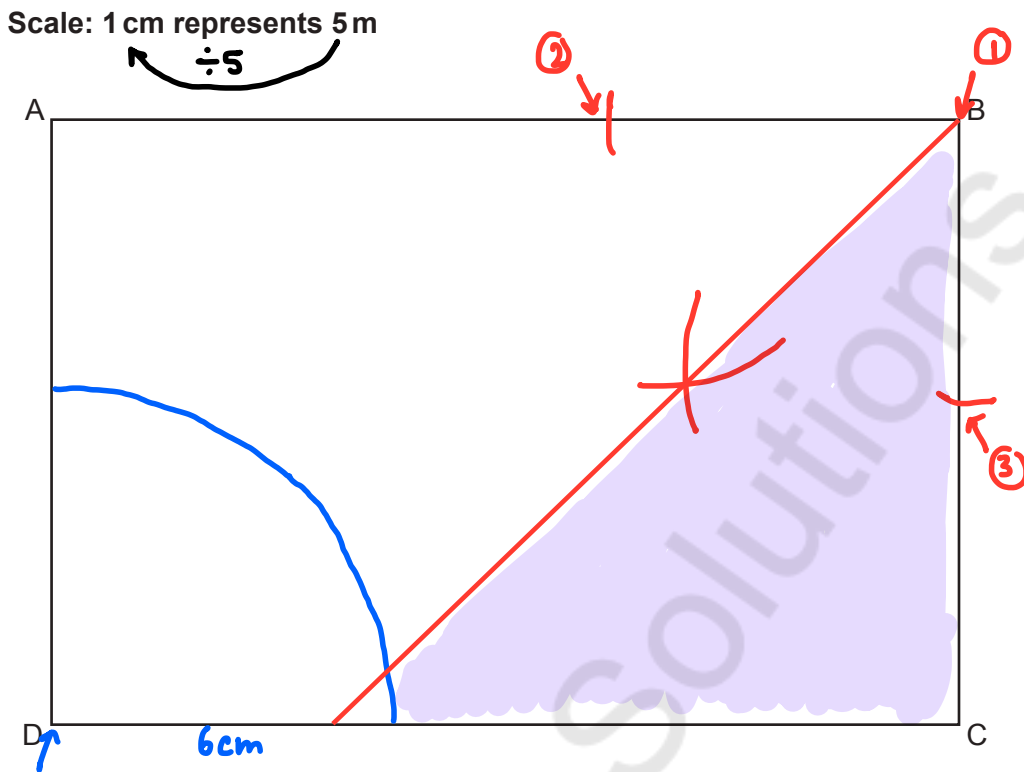


2 hours 20 minutes

$$8.30 \text{ am} + 2\text{h } 20 \text{ mins} = 10.50\text{am}$$

..... 10.50am [4]

19 The scale drawing shows Katy's garden ABCD.



Katy places a statue in the garden.

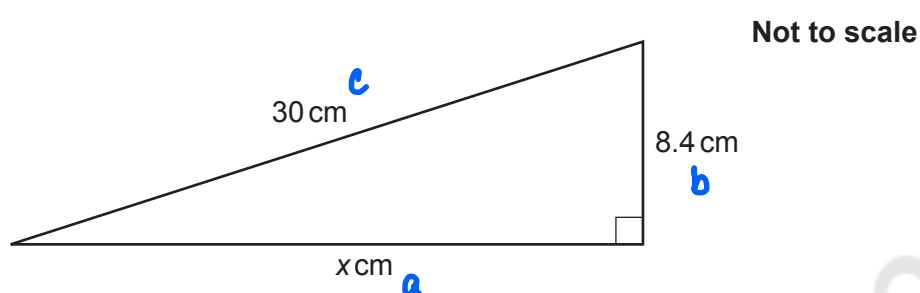
The statue is $\div 5$ 6cm

- more than 30m from D
- closer to CB than AB. *Angle bisector*

Construct and shade the region where the statue could be placed.
Show all your construction lines.

[5]

20 Here is a right-angled triangle.



Work out the value of x .

$$a^2 + b^2 = c^2$$

$$\begin{aligned} x^2 + 8.4^2 &= 30^2 \\ - 8.4^2 &\quad - 8.4^2 \end{aligned}$$

$$x^2 = 30^2 - 8.4^2$$

$$\sqrt{\quad} \quad \sqrt{\quad}$$

$$x = \sqrt{30^2 - 8.4^2}$$

$$= 28.8$$

$$x = \underline{28.8} \dots\dots\dots [3]$$

23 Here are the interest rates for two bank accounts.

Northern Savings Bank (NSB)
2.5% per year
compound interest

Central Alliance Bank (CAB)
2.7% per year
simple interest

$$\text{Final} = \text{investment} \times \text{multiplier}^n$$

Mia puts £6400 in each account.

Calculate the difference in value between the two accounts after 8 years.
Give your answer correct to the nearest penny.

NSB

$$\begin{aligned} \text{Multiplier} &= 100 + 2.5 \\ &= 102.5\% \\ &\quad \downarrow \div 100 \\ &= 1.025 \end{aligned}$$

$$\begin{aligned} &6400 \times 1.025^8 \\ &= 7797.778544 \\ &\approx \text{£}7797.78 \end{aligned}$$

CAB

$$2.7\% \xrightarrow{\div 100} 0.027$$

$$0.027 \times 6400 = \text{£}172.80$$

$$172.80 \times 8 = \text{£}1382.40$$

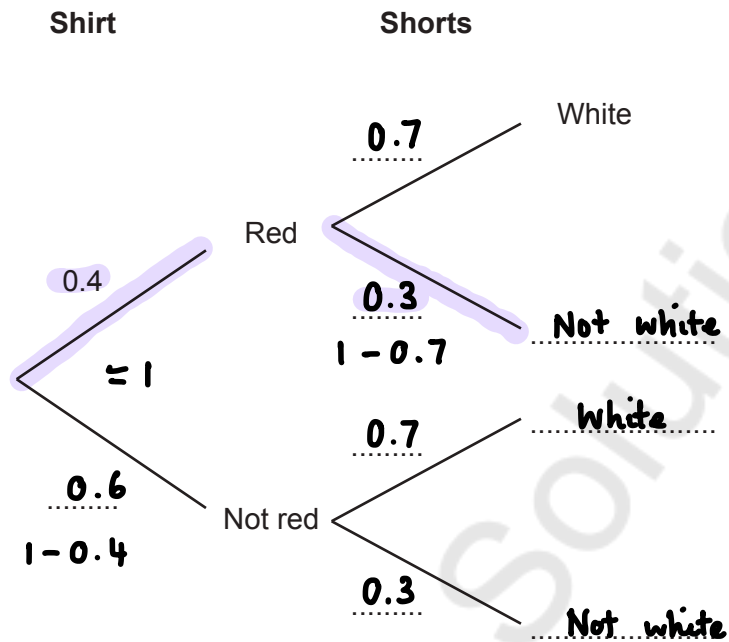
$$6400 + \text{£}1382.40 = \text{£}7782.40$$

$$\begin{aligned} \text{Difference} &= 7797.78 - 7782.40 \\ &= 15.38 \end{aligned}$$

£ **15.38** [6]

- 24 Romelu picks a shirt and shorts.
The probability he picks a red shirt is 0.4.
The probability he picks white shorts is 0.7.

(a) Complete the tree diagram.



[3]

- (b) Calculate the probability that Romelu picks a red shirt but does not pick white shorts.

$$0.4 \times 0.3 = 0.12$$

(b) 0.12 [2]

- 25 Marcin buys 7 rulers and 15 crayons for £7. A ruler costs 12p more than a crayon.

18

700p

x100

Find the cost of one crayon.

$$\text{Crayon} = c$$

$$\text{Ruler} = c + 12$$

$$7(c + 12) + 15c = 700$$

$$7c + 84 + 15c = 700$$

$$22c + 84 = 700$$

$$- 84 \quad - 84$$

$$22c = 616$$

$$\div 22 \quad \div 22$$

$$c = 28$$

cost of one crayon =**28**..... p [5]

26 Here are the first four terms of a sequence.

$$33 \quad 28 \quad 23 \quad 18 \quad 13$$

$\swarrow +5$ $\swarrow -5$ $\swarrow -5$ $\swarrow -5$

Find the n th term of the sequence.

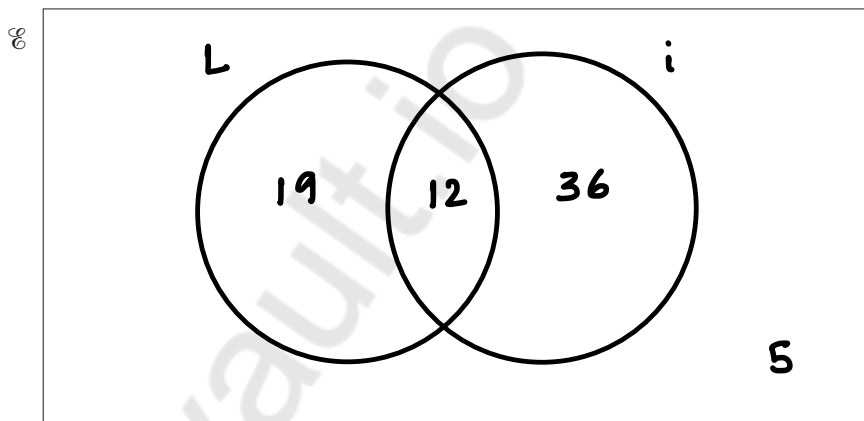
$$-5n + 33$$

..... $-5n + 33$ [2]

27 72 children are asked whether they have a laptop or an iPad.

- 31 have a laptop. ✓ $31 - 12 = 19$
- 48 have an iPad. $48 - 12 = 36$
- 12 have both. ✓
- 5 have neither. ✓

(a) Represent this information on a Venn diagram.



[3]

(b) One of the children is chosen at random.

Write down the probability that they have an iPad but not a laptop.

$$\frac{36}{72}$$

(b) [2]

