

Surname	Centre Number	Candidate Number
Other Names		0



GCSE – NEW

3300U30-1



MATHEMATICS
UNIT 1: NON-CALCULATOR X
INTERMEDIATE TIER

TUESDAY, 13 JUNE 2017 – MORNING

1 hour 45 minutes

ADDITIONAL MATERIALS

The use of a calculator is not permitted in this examination.
A ruler, protractor and a pair of compasses may be required.

INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.

You may use a pencil for graphs and diagrams only.

Write your name, centre number and candidate number in the spaces at the top of this page.

Answer **all** the questions in the spaces provided.

If you run out of space, use the continuation page at the back of the booklet, taking care to number the question(s) correctly.

Take π as 3.14.

INFORMATION FOR CANDIDATES

You should give details of your method of solution when appropriate.

Unless stated, diagrams are not drawn to scale.

Scale drawing solutions will not be acceptable where you are asked to calculate.

The number of marks is given in brackets at the end of each question or part-question.

In question 9, the assessment will take into account the quality of your linguistic and mathematical organisation, communication and accuracy in writing.

For Examiner's use only		
Question	Maximum Mark	Mark Awarded
1.	6	
2.	3	
3.	4	
4.	3	
5.	2	
6.	4	
7.	6	
8.	5	
9.	7	
10.	6	
11.	5	
12.	4	
13.	3	
14.	3	
15.	3	
16.	5	
17.	4	
18.	2	
19.	5	
Total	80	

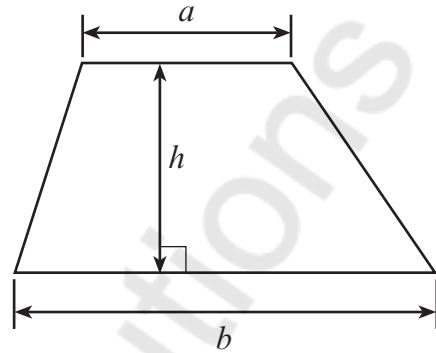
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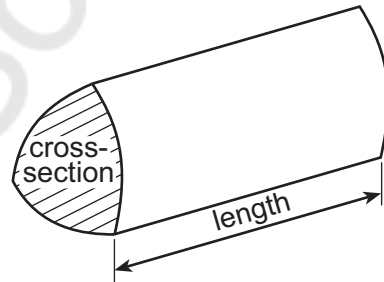
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Formula List – Intermediate Tier

$$\text{Area of trapezium} = \frac{1}{2}(a + b)h$$



$$\text{Volume of prism} = \text{area of cross-section} \times \text{length}$$



1. (a) Write down the next two numbers in the following sequence. [2]

35, -10 25, -9 16, -8 8, -7 1, -6 -5

1, -5 //

- (b) Find the value of $2x + 7y$ when $x = -3$ and $y = 10$. [2]

$$\begin{aligned} 2x + 7y & \quad x = -3 \quad y = 10 \\ 2x - 3 + 7 \times 10 & \\ -6 + 70 & = \underline{64} \end{aligned}$$

- (c) Simplify the expression $8k + 3m - 2k - 8m$. [2]

$$\begin{aligned} 8k + 3m - 2k - 8m & \quad \text{Collect like terms} \\ 8k - 2k + 3m - 8m & \\ \underline{6k - 5m} & \end{aligned}$$

2. Write down 0.4, 15% and $\frac{7}{20}$ in ascending order. [3]

You must show all your working.

0.4 to percentage

$$0.4 \times 100 = 40\%$$

15%

$\frac{7}{20}$ to percentage

$$\frac{7}{20} \times 100 = 35\%$$

15%

$\frac{7}{20}$

0.4

Smallest value



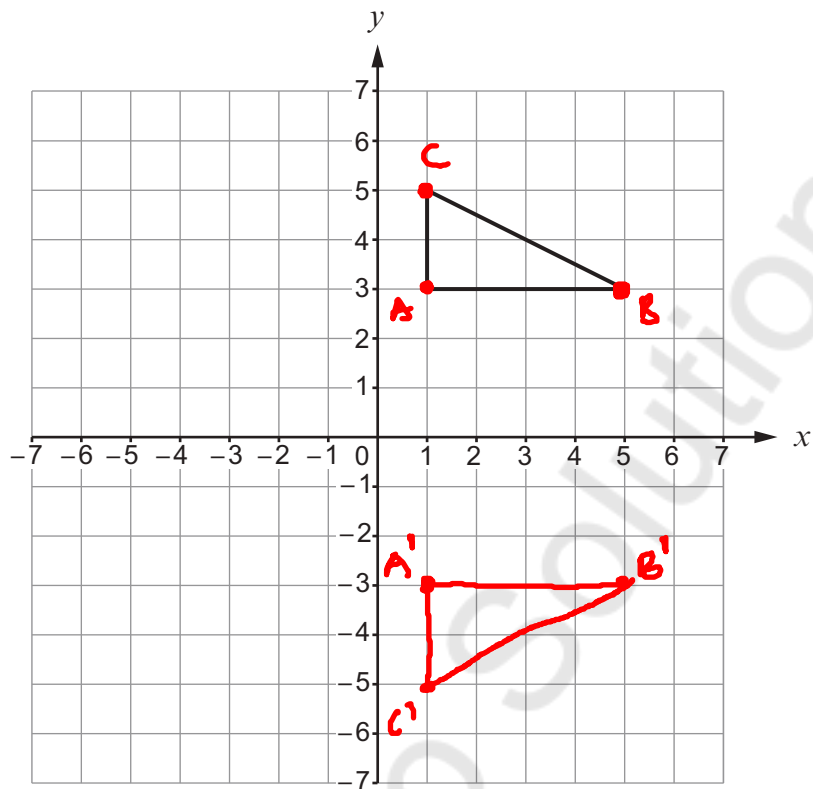
Greatest value

0.4 15% $\frac{7}{20}$
40% 15% 35%



3. (a) Reflect the triangle below in the x -axis.

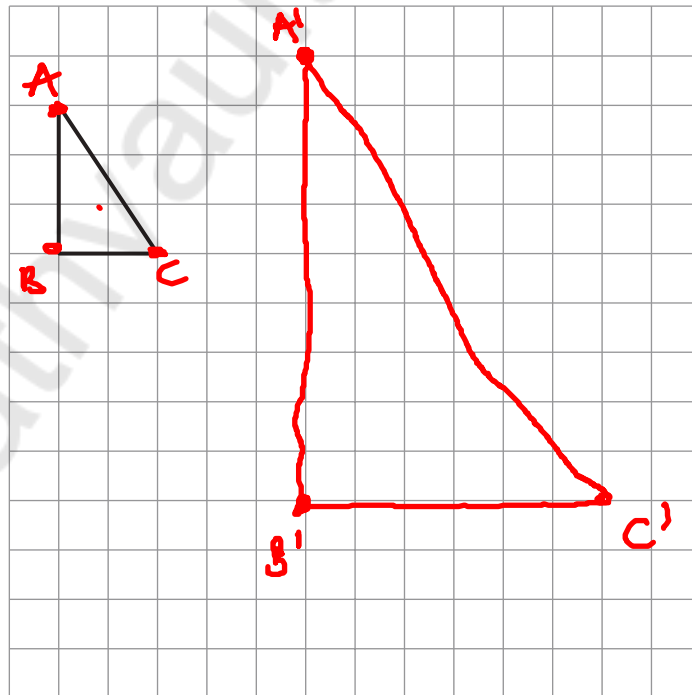
[1]



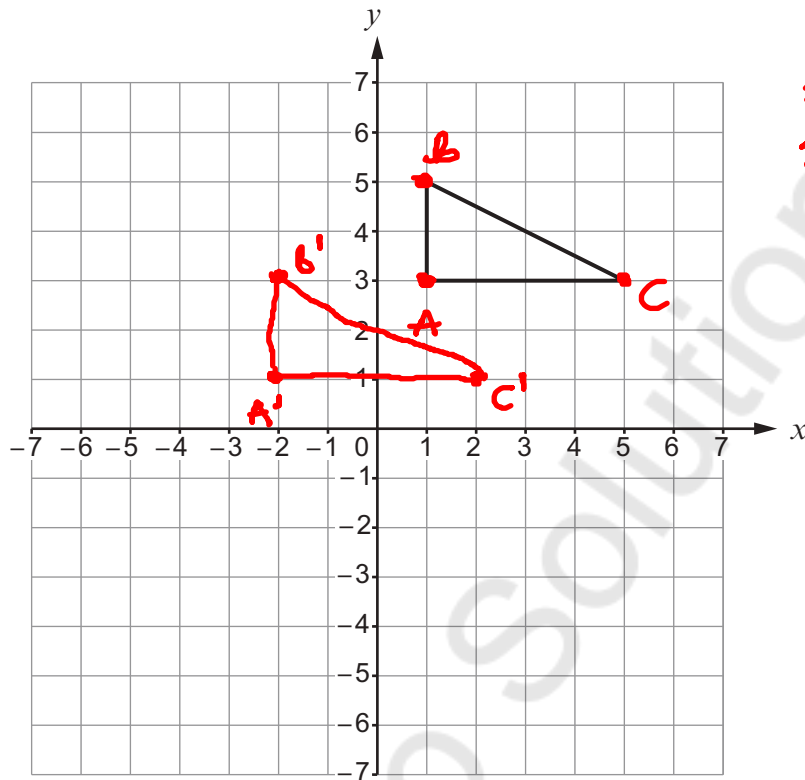
- (b) Enlarge the triangle below by a scale factor of 3.

[2]

3x3
2x3
6



(c) Translate the triangle below 3 squares to the left and 2 squares down. [1]



dice: [1, 2, 3, 4, 5, 6]

4. (a) A fair, six-sided dice is rolled.
What is the probability that a 4 is shown on the dice?
Circle your answer.

$Pr(4) = \frac{1}{6}$

- 6%
- $\frac{1}{5}$
- $\frac{1}{4}$
- 6:1
- $\frac{1}{6}$

[1]

(b) 50 raffle tickets were sold at a charity event.
Sian has a 20% chance of winning the top prize.
How many tickets did Sian buy?
Circle your answer.

- 1
- 2
- 4
- 10
- 20

[1]

total ticket sold = 50

Sian bought: 20% of 50 ticket

$\frac{20}{100} \times 50 = 10 //$

(c) A bag contains a mixture of blue beads, yellow beads and pink beads.
One bead is taken at random from the bag.

The probability that the bead is pink is $\frac{1}{5}$.

Which of the following sets of beads could have been in the bag?
Circle your answer.

[1]



$Pr(\text{pink}) = \frac{1}{5}$

First bag: $Pr(P) = \frac{3}{15} = \frac{1}{5} \checkmark$

Second bag: $Pr(P) = \frac{5}{15} = \frac{1}{3} \times$

Third bag: $Pr(P) = \frac{5}{7}$

Fourth bag: $Pr(P) = \frac{1}{11} \times$

Fifth bag: $Pr(P) = \frac{6}{15} = \frac{2}{5} \times$

6 blue
6 yellow
3 pink //



5. Team A and Team B play in a competition.

Team A has nine more points than Team B. ✓

Team A has four times as many points as Team B. ✓

How many points does each team have?

[2]

Let Team B have x points

Therefore Team A will have $x + 9$ points

Also, Team A have $4 \times x = 4x$ points

$$\begin{aligned} \text{Team A} &= \text{Team A} \\ x + 9 &= 4x \end{aligned}$$

Team A: 12 points

Team B: 3 points

$$\begin{array}{r} x + 9 = 4x \\ -x \quad -x \end{array}$$

$$\frac{9}{3} = \frac{3x}{3}$$

$$3 = x$$

Team B has 3 points

Team A has 12 points //



6. ^M David, ^F Jane and ^F Mary are beach inspectors.
Three beaches, Harlech, Rhyl and Porthcawl, are all to be inspected on a certain day.
It is decided to share the work so that the inspectors will visit one beach each, chosen at random.

- (a) List all the possible different ways they could share the work.
One has been done for you.

$$3! = 3 \times 2 \times 1 = 6 \quad [2]$$

- ① David → Harlech, Jane → Rhyl ✓ and Mary → Porthcawl
- ② David → Harlech Jane → Porthcawl Mary → Rhyl ✓
- ③ Jane → Harlech David → Porthcawl Mary → Rhyl ✓
- ④ Jane → Harlech David → Rhyl Mary → Porthcawl
- ⑤ Mary → Harlech David → Rhyl Jane → Porthcawl
- ⑥ Mary → Harlech David → Porthcawl Jane → Rhyl ✓

- (b) What is the probability that one of the female inspectors will visit Rhyl? [2]

$$\begin{aligned} \text{Pr}(\text{Female inspector visiting Rhyl}) &= \frac{4}{6} \\ &= \frac{4}{6} = \frac{2}{3} \end{aligned}$$



7. ABCD is a quadrilateral.

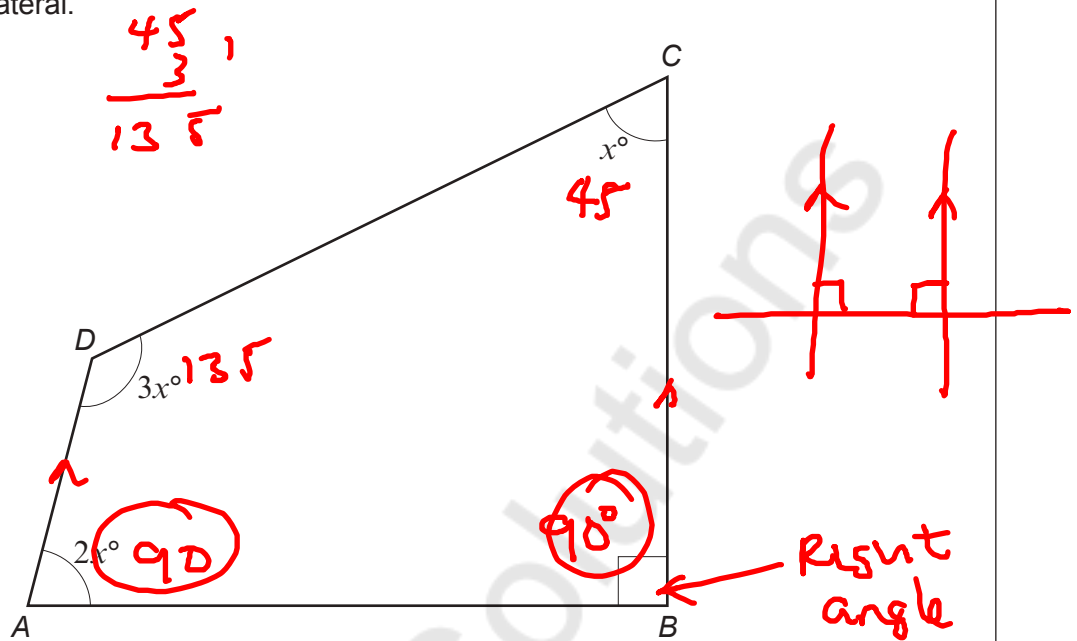


Diagram not drawn to scale

Handwritten calculations:

$$\begin{array}{r} 45 \\ 3 \\ \hline 135 \end{array}$$

$$\begin{array}{r} 45 \\ 6 \overline{) 270} \\ \underline{-24} \\ 30 \\ \underline{-30} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \overline{) 60} \\ \underline{40} \\ 20 \\ \underline{20} \\ 0 \end{array}$$

(a) Calculate the value of x .

[4]

Sum of angle in a quadrilateral = 360°

$$3x + 2x + x + 90 = 360$$

$$6x + 90 = 360$$

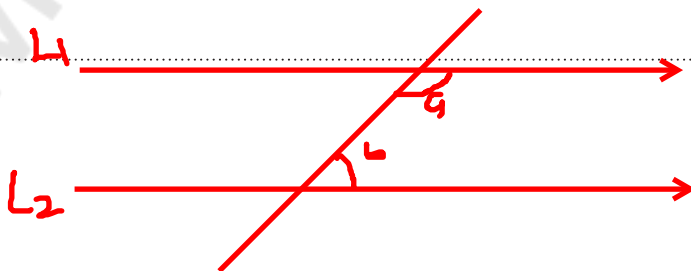
$$\quad \quad -90 \quad -90$$

$$\frac{6x}{6} = \frac{270}{6} \quad \quad x = \underline{\underline{45^\circ}}$$

(b) When ABCD is drawn to scale, would the lines AD and BC be parallel or not? You must justify your answer without using a scale drawing.

[2]

AD will be parallel to BC because the sum of the interior angle of a transversal is always 180° . If the lines are parallel



$a + b = 180^\circ$
Then, $L_1 \parallel L_2$



8. (a) Estimate the value of $\frac{41.3 \times 29.6}{198.7}$.

You must show all your working.

[2]

$$\frac{41.3 \times 29.6}{198.7} = \frac{40 \times 30}{200} = \frac{12}{2} = 6$$

$$= 6 //$$

(b) Given that $54 \times 84.2 = 4546.8$, write down the exact value of each of the following.

(i) $540 \times 842 = 454680$ [1]

(ii) $\frac{4546.8}{5.4} = 842$ [1]

(iii) $\frac{454.68}{84.2} = 5.4$ [1]

$$54 \times 84.2 = 4546.8$$

$$\frac{54 \times 84.2}{10} = \frac{454.68 \times 10}{10}$$

$$\frac{5.4 \times \cancel{84.2}}{\cancel{84.2}} = \frac{454.68}{84.2}$$

$$5.4 = \frac{454.68}{84.2}$$



9. In this question, you will be assessed on the quality of your organisation, communication and accuracy in writing.

In the diagram below,

- $ABCD$ is a rectangle, and
- PQ is parallel to AD .

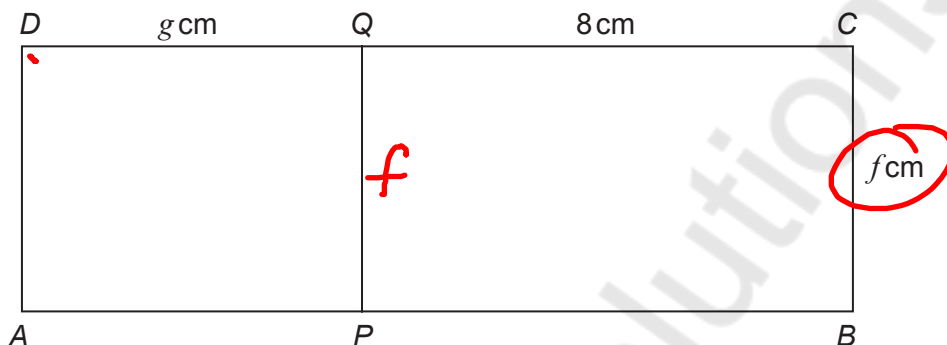


Diagram not drawn to scale

The area of $ABCD$ is 52 cm^2 .
The area of $APQD$ is 20 cm^2 .

Calculate the values of f and g .
You must show all your working.

[5 + 2 OCW]

Area of rectangle $ABCD = \text{Length} \times \text{width}$

$$\text{Length} = CD = g + 8 \text{ cm}$$

$$\text{width} = CB = f \text{ cm}$$

$$\begin{aligned} \text{Area of } ABCD &= (g+8) \times f \\ 52 &= gf + 8f \quad \text{--- (1)} \end{aligned}$$

Also, Area of rectangle $APQD = \text{length} \times \text{width}$

$$\text{Length} = DQ = g \text{ cm}$$

$$\text{width} = QP = f \text{ cm}$$

$$\begin{aligned} \text{Area of } APQD &= g \times f = gf \\ 20 &= gf \quad \text{--- (2)} \end{aligned}$$

Substitute $gf = 20$ into equation (1)

$$\begin{aligned} 52 &= 20 + 8f \\ -20 &\quad -20 \end{aligned}$$

$$\frac{32}{8} = \frac{8f}{8}$$

$$4 = f$$

$$\text{Since, } gf = 20$$

$$\frac{4g}{4} = \frac{20}{4}$$

$$f = 4 \text{ cm} \quad g = 5 \text{ cm}$$

$$g = 5 //$$



10. Ceri has a set of cards.
Each of her cards is labelled North, East, South or West. N E S W

- (a) Ceri chooses one card at random from her set of cards.
Complete the table below to find the probability of Ceri choosing a card labelled West. [2]

Label	North	East	South	West
Probability	0.4	0.25	0.2	0.15

$$P(N) + P(E) + P(S) + P(W) = 1$$

$$0.4 + 0.25 + 0.2 + P(W) = 1$$

$$0.85 + P(W) = 1$$

$$P(W) = 1 - 0.85 = 0.15$$

- (b) Ceri chooses one card at random from her set of cards.

What is the probability that the card is labelled East or South? [2]

$$P(E \text{ or } S) = P(E) + P(S)$$

$$P(E \text{ or } S) = 0.25 + 0.2 = \underline{\underline{0.45}}$$

- (c) Sasha has an identical set of cards.
Ceri and Sasha each choose one card at random from their set of cards.

What is the probability that they both choose a card labelled North? [2]

$$Pr(N \text{ and } N) = P(N) \times P(N)$$

$$= 0.4 \times 0.4$$

$$= \frac{4}{10} \times \frac{4}{10} = \frac{16}{100}$$

$$\underline{\underline{0.16}}$$



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$3^2 = 3 \times 3$

Examiner only

11. The table below shows some of the values of $y = x^2 - 5x + 2$, for values of x from -1 to 5 .

x	-1	0	1	2	<u>3</u>	4	5
$y = x^2 - 5x + 2$	8 ✓	2 ✓	-2 ✓	-4 ✓	-4 ✓	-2 ✓	2 ✓

(a) Complete the table above.

$x = 3$

[1]

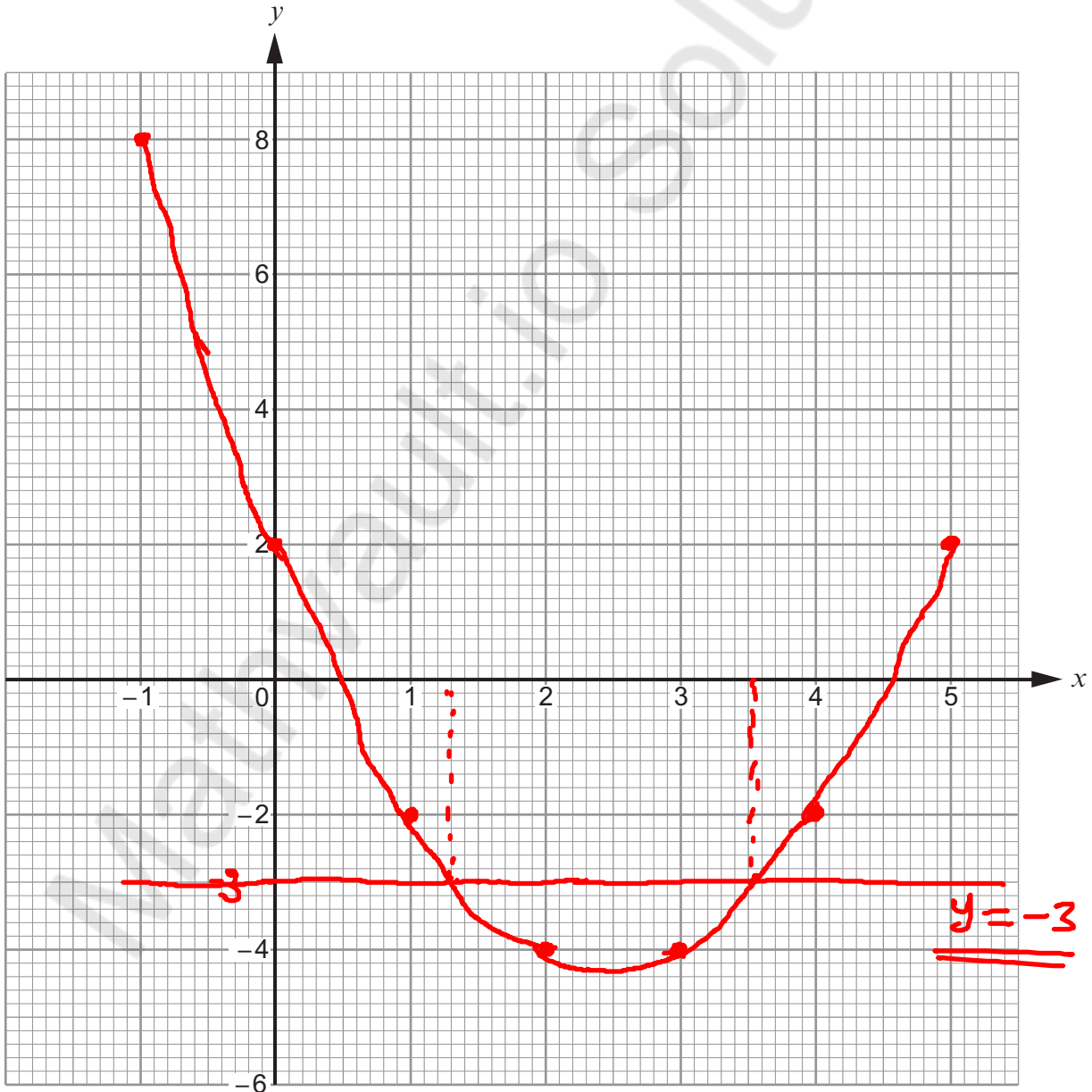
$y = x^2 - 5x + 2 \quad y = 3^2 - 5 \times 3 + 2 = 9 - 15 + 2$

$y = -6 + 2 = -4$

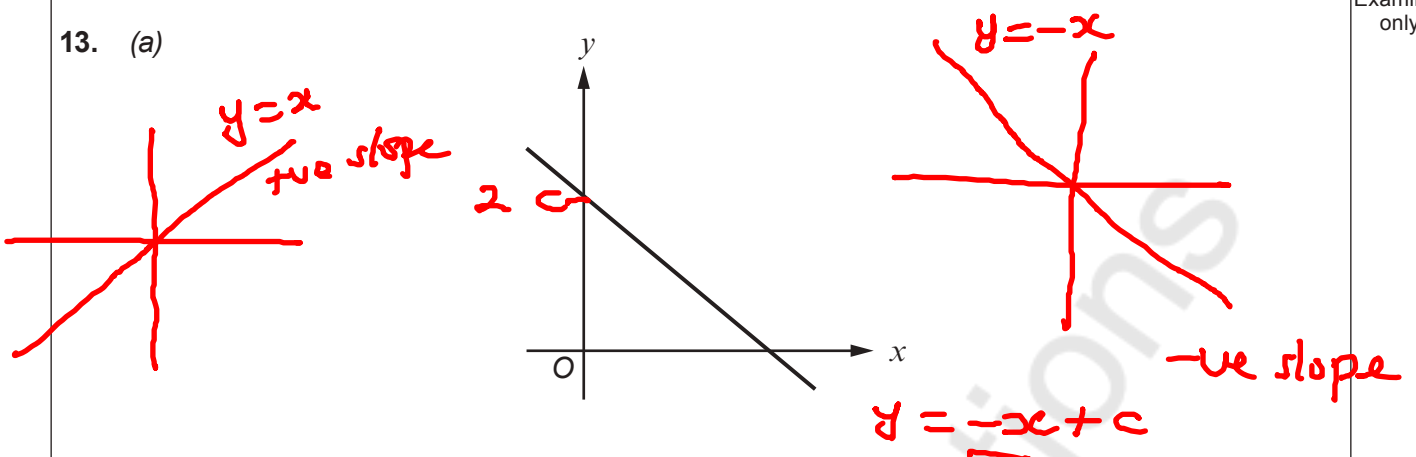
(b) On the graph paper below, draw the graph of $y = x^2 - 5x + 2$ for values of x from -1 to 5 .

[2]

French curve



13. (a)



Which **one** of the following equations could represent the line shown in the graph above?
Circle your answer. [1]

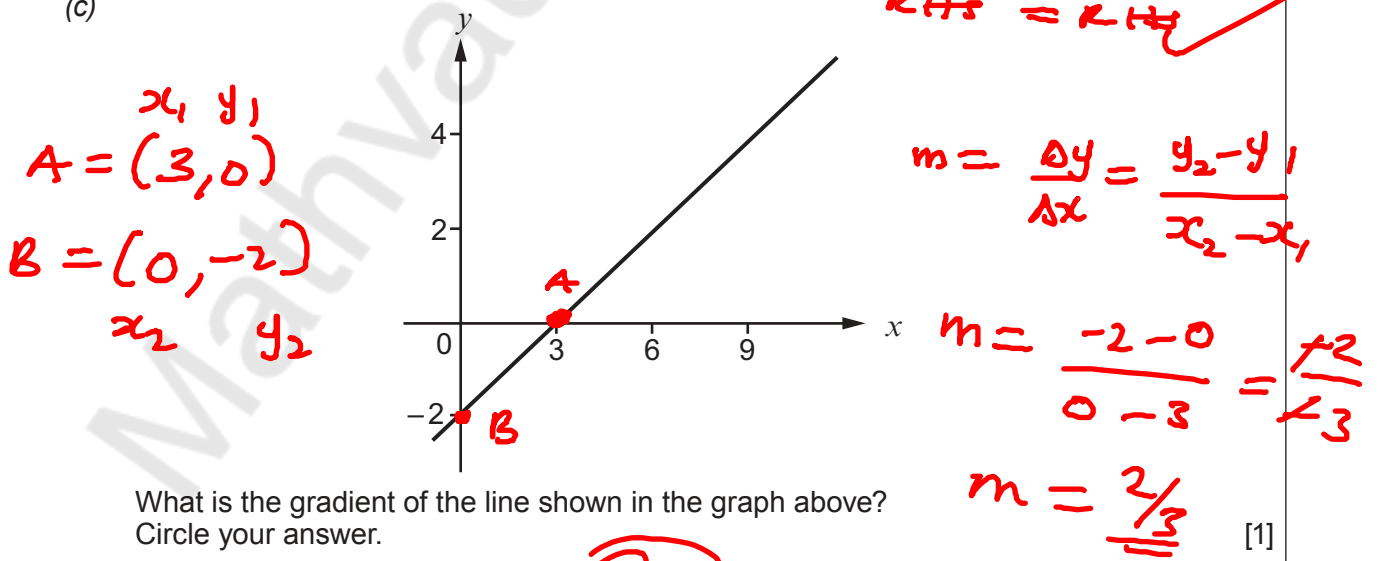
- ~~$y = -x - 2$~~ $y = -x + 2$ ~~$y = x + 2$~~ ~~$y = x - 2$~~ $y = -x$

(b) Which **one** of the following points lies on the line $2y = 3x + 4$?
Circle your answer. [1]

- ~~$(2, -5)$~~ ~~$(5, 2)$~~ ~~$(-2, 5)$~~ $(2, 5)$ ~~$(-2, -5)$~~

① $2y = 3x + 4$ ② $2 \times 2 = 3 \times 5 + 4$ ③ $2 \times 5 = 3 \times -2 + 4$
 $2 \times -5 = 3 \times 2 + 4$ $4 = 19$ $10 = -2$
 $-10 = 10$ LHS \neq RHS LHS \neq RHS
 LHS \neq RHS ④ $2 \times 5 = 3 \times 2 + 4$
 $10 = 10$
 RHS = RHS ✓

(c)



What is the gradient of the line shown in the graph above?
Circle your answer. [1]

- $\frac{3}{2}$ $-\frac{3}{2}$ $\frac{2}{3}$ $-\frac{2}{3}$ -6



14. A whole number is written on a card.

You are given three clues to help you work out the number on the card.

Clue 1 : **Double** the number is between 8 and 18 inclusive.

Clue 2 : The number is a prime number.

Clue 3 : The number is **not** a factor of 100.

What is the number on the card?

You must show all your working.

[3]

A whole number is a number without a decimal point

Clue 1: Double of the number is between 8 and 18 incl

Let the number be

number =	1	2	3	4	5	6	7	8	9	10
Double =	2	4	6	8	10	12	14	16	18	20

So, from the first clue, the number can be 4, 5, 6, 7, 8, 9.

Clue 2: The number is a prime number
The prime number from Clue 1 answers are: 5, 7

The number on the card is 7

Clue 3: The number is not a factor of 100

Since 5 is a factor of 100. Then the number on the card is 7

7



15. In the following formulae, each measurement of length is represented by a letter.

Consider the dimensions implied by the formulae.

Write down, for each case, whether the formula could be for a length, an area, a volume or none of these.

The first one has been done for you.

[3]

<u>Formula</u>	<u>Formula could be for</u>
$d^2 + hw$
$L^2 + L^2 = L^2$ volume
$d + w + h$ Area
$L + L + L = L$ Length
$2\pi r - \pi r^2$ none of these
$(d + h)w$ Area
$d^3 + dwh$ Volume

$$(d+h)w$$

$$dw + hw$$

$$L^2 + L^2 = L^2$$

$$d^3 + dwh$$

$$L^3 + L^3$$

$$= L^3$$

Length $\rightarrow L$

Area $\rightarrow L^2$

Volume $\rightarrow L^3$

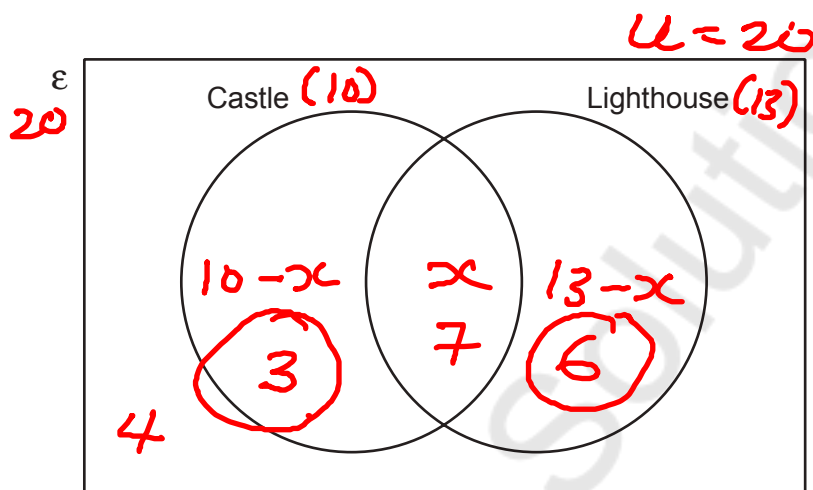


16. A group of 20 people visited Anglesey for a weekend break.

- 10 of the group visited Beaumaris Castle.
- 13 of the group visited South Stack Lighthouse.
- 4 of the group did not visit either of these places.

(a) Complete the Venn diagram below to show this information.
The universal set, ϵ , contains all of the 20 people in the group.

[3]



$$10 - x + x + 13 - x + 4 = 20$$

$$27 - x = 20$$

$$27 - 20 = x$$

$$7 = x$$

$$x = 7$$

(b) One person is chosen at random from the group.
What is the probability that this person visited only one of the two places?

[2]

$$\text{Pr}(\text{visiting only one of the two places}) = \frac{9}{20}$$



17. Solve the following simultaneous equations using an algebraic (not graphical) method. [4]

$$\text{LCM} = 12$$

$$\begin{aligned} 3x + 4y &= 7 & \text{--- (i)} \\ 2x - 3y &= 16 & \text{--- (ii)} \end{aligned}$$

Using elimination method: eliminating y

$$\begin{array}{r} 16 \ 2 \\ \times 4 \\ \hline 64 \end{array}$$

$$\begin{array}{r} 3x + 4y = 7 \quad \times 3 \\ 2x - 3y = 16 \quad \times 4 \\ \hline 9x + 12y = 21 \quad \text{--- (iii)} \\ + \quad 8x - 12y = 64 \quad \text{--- (iv)} \\ \hline 17x = 85 \end{array}$$

$$17x = 85$$

$$\frac{17x}{17} = \frac{85}{17}$$

$$\begin{array}{r} 17 \ 3 \\ \times 5 \\ \hline 85 \end{array}$$

$$\underline{\underline{x = 5}}$$

Using equation (i)

$$3x + 4y = 7$$

$$3 \times 5 + 4y = 7$$

$$15 + 4y = 7$$

$$\begin{array}{r} -15 \\ -15 \end{array}$$

$$\frac{4y}{4} = \frac{-8}{4}$$

$$y = \underline{\underline{-2}}$$

$$x = 5, \quad y = -2 //$$



18. Calculate the value of $(5.41 \times 10^5) + (2.3 \times 10^4)$.
Give your answer in standard form.

$$10^4 = \frac{10^5}{10^1}$$

[2]

$$5.41 \quad 5.41 \times 10^5 + 2.3 \times 10^4$$

$$\underline{0.23} \quad 5.41 \times 10^5 + 2.3 \times \frac{10^5}{10}$$

$$5.64$$

$$ax + bx \\ x[a+b]$$

$$5.41 \times 10^5 + 0.23 \times 10^5$$

$$10^5(5.41 + 0.23) = \underline{\underline{5.64 \times 10^5}}$$

19. Rashid owned n sheep.
Eifion had exactly 4 times as many sheep as Rashid.

Rashid buys 17 extra sheep.
Eifion sells 8 of his sheep.

Eifion still has more sheep than Rashid.

Form an inequality, in terms of n .
Solve the inequality to find the **least** value of n .
You must show all your working.

[5]

$$\text{Rashid} = n \text{ sheep}$$

$$\text{Eifion} = 4 \times n \text{ sheep}$$

$$\text{Rashid bought extra } 17$$

$$\text{Rashid (new)} = n + 17 \text{ sheep}$$

$$\text{Eifion sold } 8 \text{ sheep.}$$

$$\text{Eifion (new)} = 4n - 8$$

$$\text{Eifion (sheep)} > \text{Rashid (sheep)}$$

$$(i) \quad 4n - 8 > n + 17$$

$$-n + 8 \quad -n + 8$$

$$\frac{3n}{3} > \frac{25}{3}$$

$$n > 8\frac{1}{3}$$

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The least value of n is 9

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