

Surname	Centre Number	Candidate Number
Other Names		0



**GCSE**

3300U40-1



**MATHEMATICS**  
**UNIT 2: CALCULATOR-ALLOWED**  
**INTERMEDIATE TIER**

THURSDAY, 7 JUNE 2018 – MORNING

1 hour 45 minutes

**ADDITIONAL MATERIALS**

A calculator will be required for this examination.  
A ruler, protractor and a pair of compasses may be required.

**INSTRUCTIONS TO CANDIDATES**

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.  
You may use a pencil for graphs and diagrams only.  
Write your name, centre number and candidate number in the spaces at the top of this page.  
Answer **all** the questions in the spaces provided.  
If you run out of space, use the continuation page at the back of the booklet. Question numbers must be given for all work written on the continuation page.  
Take  $\pi$  as 3.14 or use the  $\pi$  button on your calculator.

**INFORMATION FOR CANDIDATES**

You should give details of your method of solution when appropriate.  
Unless stated, diagrams are not drawn to scale.  
Scale drawing solutions will not be acceptable where you are asked to calculate.  
The number of marks is given in brackets at the end of each question or part-question.  
In question 8, the assessment will take into account the quality of your linguistic and mathematical organisation, communication and accuracy in writing.

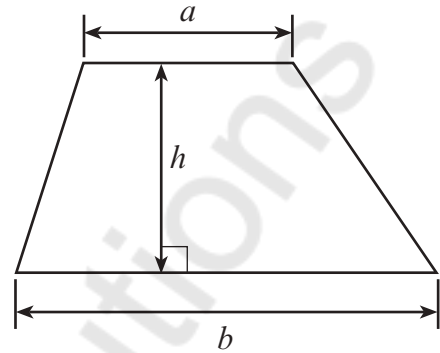
For Examiner's use only		
Question	Maximum Mark	Mark Awarded
1.	6	
2.	3	
3.	4	
4.	3	
5.	4	
6.	3	
7.	4	
8.	6	
9.	3	
10.	4	
11.	4	
12.	3	
13.	4	
14.	4	
15.	3	
16.	5	
17.	6	
18.	5	
19.	6	
<b>Total</b>	<b>80</b>	



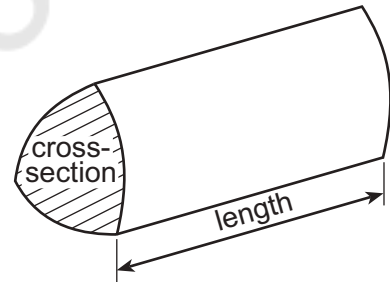
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## Formula List – Intermediate Tier

**Area of trapezium** =  $\frac{1}{2}(a + b)h$



**Volume of prism** = area of cross-section  $\times$  length



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ON THIS PAGE**

Mathvaudio Solutions



1. (a) Solve  $\frac{x}{4} = 7$ . [1]

$$\frac{x}{4} = 7 \quad x = 7 \times 4 = 28$$

(b) Simplify  $3f + 7g + f - 4g$ . [2]

$$3f + f + 7g - 4g = 4f + 3g$$

(c) Use the formula  $5p + 2q = t$  to find the value of  $q$  when  $p = 4$  and  $t = 24.6$ . [3]

$$5(4) + 2q = 24.6$$

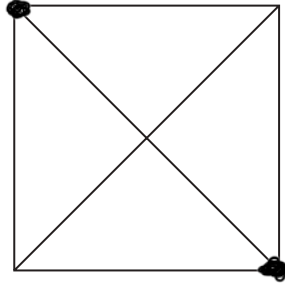
$$2q = 24.6 - 20$$

$$2q = 4.6$$

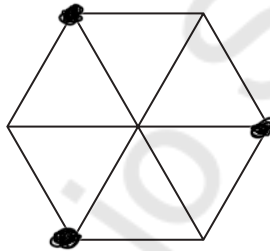
$$q = \frac{4.6}{2} = 2.3$$



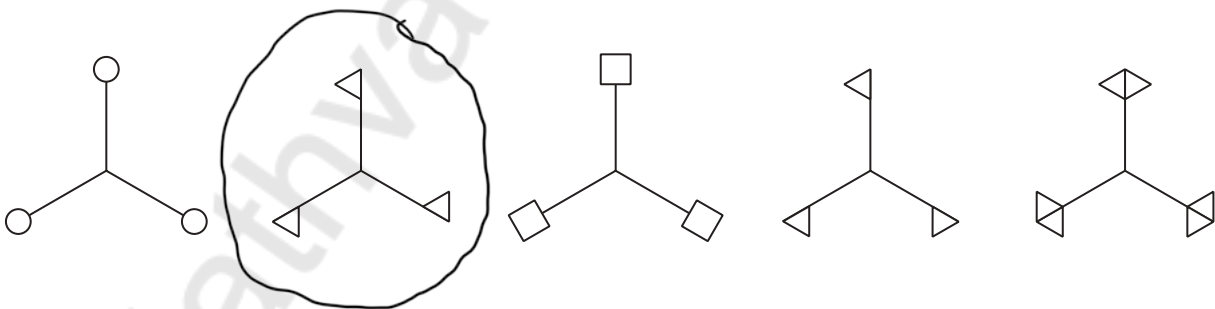
2. (a) The square drawn below has rotational symmetry of order 4.  
Place **two** identical dots (●) on the square so that it will have rotational symmetry of order 2. [1]



- (b) The regular hexagon drawn below has rotational symmetry of order 6.  
Place **three** identical dots (●) on the regular hexagon so that it will have rotational symmetry of order 3. [1]



- (c) Which of the following shapes has rotational symmetry of order 3, but has **no** line symmetry?  
Circle the correct shape. [1]



3. A travel company offers the following holiday options.

Time	Accommodation	Transport
Summer or Winter	Cottage or Hotel	Train or Bus or Car

- (a) List all the possible different combinations of holiday options that the company offers. One has been done for you. [3]

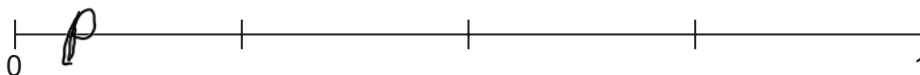
<u>Time</u>	<u>Accommodation</u>	<u>Transport</u>
Summer	Cottage	Train ✗
Summer	Cottage	Bus
Summer	Cottage	Car
Summer	Hotel	Train
Summer	Hotel	Bus
Summer	Hotel	Car
Winter	Cottage	Train
Winter	Cottage	Bus
Winter	Cottage	Car
Winter	Hotel	Train
Winter	Hotel	Bus
Winter	Hotel	Car

- (b) A holiday is chosen at random from all the different combinations on offer. **P** is the probability that the chosen holiday is a

**Summer holiday, staying in a Cottage and travelling by Train.**

Mark the point **P** on the probability scale shown below.

[1]



4. Which of the following fractions is nearest to  $\frac{1}{4}$ ?

$$\frac{1}{5}$$

$$\frac{7}{25}$$

$$\frac{13}{50}$$

You must show all your working.

[3]

$$\frac{1}{4}, \frac{1}{5}, \frac{7}{25}, \frac{13}{50}$$

$$\frac{12.5, 10, 14, 13}{50}$$

So the closest to 12.5 is 13  
 $\therefore \frac{13}{50}$  is nearest to  $\frac{1}{4}$

Answer  $\frac{13}{50}$

5. Calculate **both** the area and the perimeter of a rectangle 6 cm long and 4.5 cm wide.

Use the answer spaces to clearly identify which is the area and which is the perimeter.  
 You must give the correct units for each of your answers.

[4]

Area

$$l \times b$$

$$6 \times 4.5$$

$$= 27 \text{ cm}^2$$

Perimeter

$$2(l+b)$$

$$2(6+4.5)$$

$$2 \times 10.5$$

$$= 21 \text{ cm}$$

Area =  $27 \text{ cm}^2$

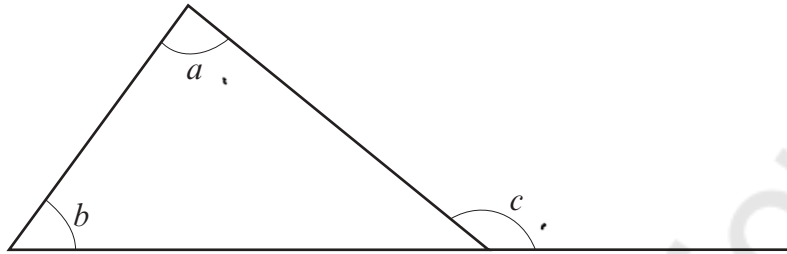
Perimeter =  $21 \text{ cm}$



6. Circle the correct equation for each of the following.  
All the lines shown are straight lines.

(a)

[1]



$a = b + c$

$b = c + a$

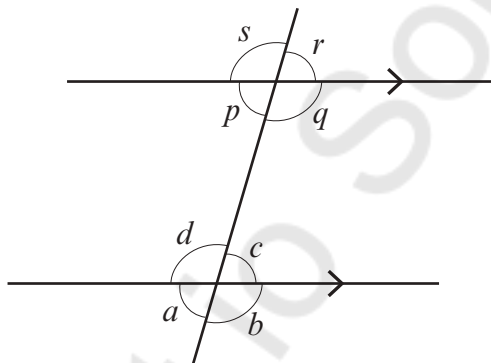
$b = a - c$

$c = a + b$

$c = a - b$

(b)

[1]



$a + c + s + q = 360^\circ$

$p + a = 180^\circ$

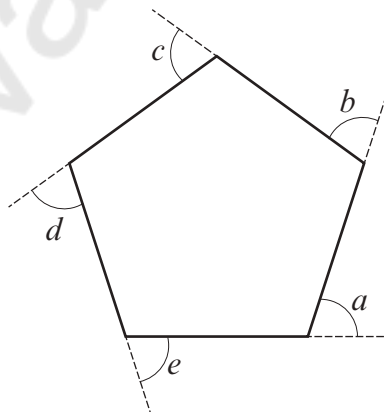
$c = q$

$d = r$

$p + q + d + c = 180^\circ$

(c)

[1]



$\frac{a + b + c + d + e}{5} = 360^\circ$

$a + b + c + d + e = \frac{360^\circ}{5}$

$a + b + c + d + e = 180^\circ$

$a + b + c + d + e = 540^\circ$

$a + b + c + d + e = 360^\circ$



7. Calculate the mean of these four time periods.  
You must give your answer in hours and minutes.

[4]

5 hours 20 minutes

2 hours 44 minutes

6 hours 18 minutes

4 hours 34 minutes

$$\text{Add the hours} = 5 + 2 + 6 + 4 = 17 \text{ hours}$$

$$\text{Add the minutes} = 20 + 44 + 18 + 34 = 116 \text{ minutes}$$

$$\text{Convert 17 hours to minutes} = 1020 \text{ minutes}$$

$$\text{Total} = 1136 \text{ minutes}$$

$$\text{Mean} = \frac{1136}{4} = 284 \text{ minutes}$$

Convert to hours & minutes

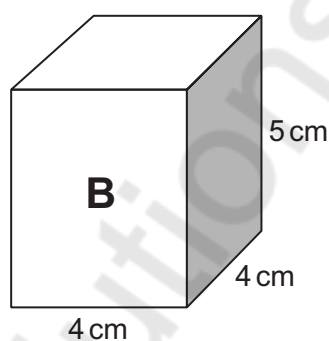
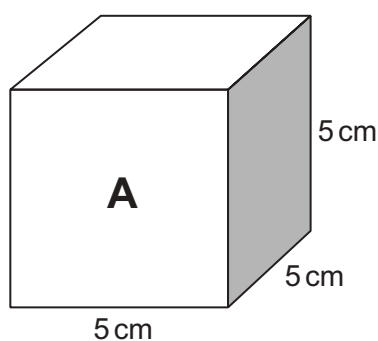
$$\frac{284}{60} = 4 \text{ hrs } \& \text{ } 44 \text{ mins}$$

$$\text{Mean time} = \overset{17}{4} \text{ hours } \overset{44}{44} \text{ minutes}$$



8. In this question, you will be assessed on the quality of your organisation, communication and accuracy in writing.

Cube **A** and cuboid **B** are shown below.



Diagrams not drawn to scale

Express the volume of **B** as a percentage of the volume of **A**.  
You must show all your working.

[4 + 2 OCW]

$$\begin{aligned} \text{Vol of A} &= (5 \times 5 \times 5) \text{ cm}^3 \\ &= 125 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Vol of B} &= (4 \times 4 \times 5) \text{ cm}^3 \\ &= 80 \text{ cm}^3 \end{aligned}$$

Vol of B expressed as a percentage of vol of A

$$\begin{aligned} &= \frac{80}{125} \times 100 \\ &= 64\% \end{aligned}$$



9. The diagram below shows an equilateral triangle  $ABC$  with  $AB = (4x - 7)$  cm.

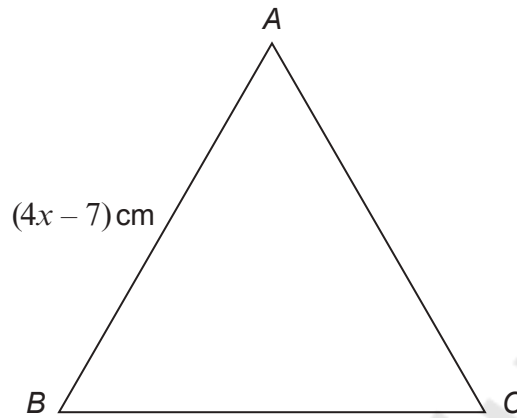


Diagram not drawn to scale

The perimeter of the triangle is 27 cm.  
Calculate the value of  $x$ .

[3]

$$\begin{aligned} \text{Perimeter} &= 27 = 3(4x - 7) \\ 12x - 21 &= 27 \\ 12x &= 27 + 21 \\ 12x &= 48 \\ x &= \frac{48}{12} \\ x &= 4 \end{aligned}$$



10. A box contains many discs, identical in shape and size.  
A picture of one of four Welsh castles is printed on each disc.

- (a) A disc is chosen at random from the box.  
Complete the table below to find the probability of choosing a disc showing Dinefwr Castle. [2]

Picture	Caernarfon Castle	Harlech Castle	Rhuddlan Castle	Dinefwr Castle
Probability	0.36	0.12	0.24	0.28

$$1 - 0.36 - 0.12 - 0.24 = 0.28$$

- (b) In the box, there were 522 discs showing a picture of Caernarfon Castle.  
How many of the discs showed a picture of Harlech Castle? [2]

Probability for Harlech Castle =  $\frac{1}{3}$

$$522 \times \frac{1}{3} = 174 \text{ discs}$$



11. (a) Calculate  $\frac{145.3}{(12.4 - 9.8)^3}$ , giving your answer correct to 3 significant figures. [2]

$$\frac{145.3}{(2.6)^3} = \frac{145.3}{17.576} = 8.2669 \approx 8.27 \quad (\text{to 3 sig figures})$$

- (b) Calculate the reciprocal of 47, giving your answer correct to 4 decimal places. [2]

$$\frac{1}{47} = 0.0213 \quad (\text{to 4 decimal places})$$

12. Circle the correct answer in each of the following.

- (a) Which of the following values **cannot** be an external angle of a regular polygon? [1]

10°

18°

30°

48°

72°

Regular polygon can't have 48°

- (b) An arrow on a spinner is facing north. It is turned clockwise through an angle of 1530°. In which direction will the arrow now be facing? [1]

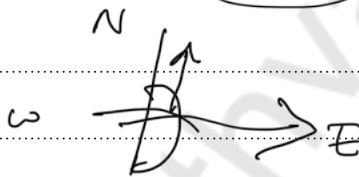
North

East

South

West

None of these



- (c) Point A is on a bearing of 100° from point B. What is the bearing of point B from point A? [1]

260°

100°

280°

180°

80°

Add 180°



13. A solution of the equation

$$x^3 - 7x - 51 = 0$$

lies between 4 and 5.

Use the method of trial and improvement to find this solution correct to 1 decimal place.  
You must show all your working.

[4]

$$x^3 - 7x - 51 = 0$$

$$x^3 - 7x = 51$$

Try 4.1 =  $(4.1)^3 - 7(4.1) = 40.221 \neq 51$

Try 4.2 =  $(4.2)^3 - 7(4.2) = 44.688 \neq 51$

Try 4.3 =  $(4.3)^3 - 7(4.3) = 49.407$

Try 4.4 =  $(4.4)^3 - 7(4.4) = 54.384$

$$\therefore 4.3 < x < 4.4$$

So  $x$  with 2 correct evaluations

$$4.3 \leq x \leq 4.35$$

Correct to 1 decimal place

$$x = \underline{\underline{4.3}}$$



14. (a) The highest common factor (HCF) of 30 and 75 is the square root of a number. What is the number? [2]

$$\begin{array}{r} 5 \overline{) 30} \quad 25 \\ 3 \overline{) 75} \quad 15 \\ \quad 2 \quad 5 \end{array} \quad \text{HCF} = 15$$

$$15^2 = 225$$

The no = 225

- (b) The cube root of 32.768 is  $33\frac{1}{3}\%$  of a number. What is the number? [2]

$$\sqrt[3]{32.768} = \sqrt[3]{\frac{4096}{125}} = \frac{16}{5}$$

$$33\frac{1}{3}\% \text{ of } x \text{ (the number)} = \frac{16}{5}$$

$$\frac{100}{3}\% \text{ of } x = \frac{16}{5}$$

$$\frac{100}{3} \times \frac{1}{100} x = \frac{16}{5}$$

$$\frac{x}{3} = \frac{16}{5}$$

$$x = \frac{16 \times 3}{5}$$

$$= \frac{48}{5}$$

$$x = 9.6$$



15.  $PQR$  is a right-angled triangle, as shown below.  
 $PQ = 1.41$  m and  $PR = 0.89$  m.

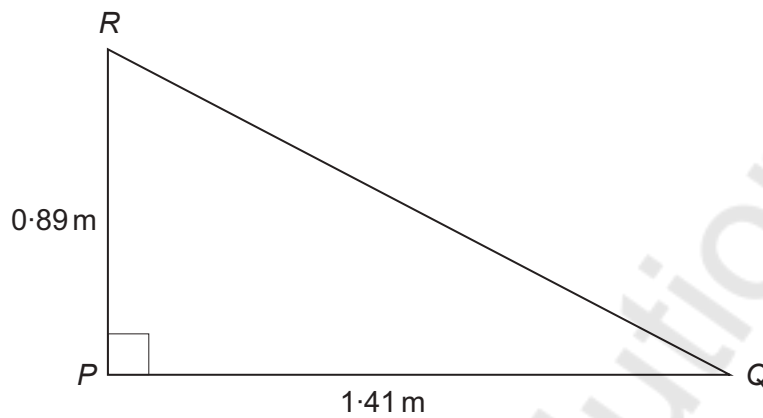


Diagram not drawn to scale

Calculate the length of  $QR$ .

[3]

Using Pythagoras Theorem

$$\begin{aligned} QR^2 &= PR^2 + PQ^2 \\ &= 0.89^2 + 1.41^2 \\ &= 2.7802 \end{aligned}$$

$$\begin{aligned} QR &= \sqrt{2.7802} \\ &= 1.67 \text{ m} \end{aligned}$$



16. Visitors to the top of Snowdon can either walk up the mountain or take the mountain railway from Llanberis.

On a particular day, a visitor to the top of Snowdon is chosen at random.

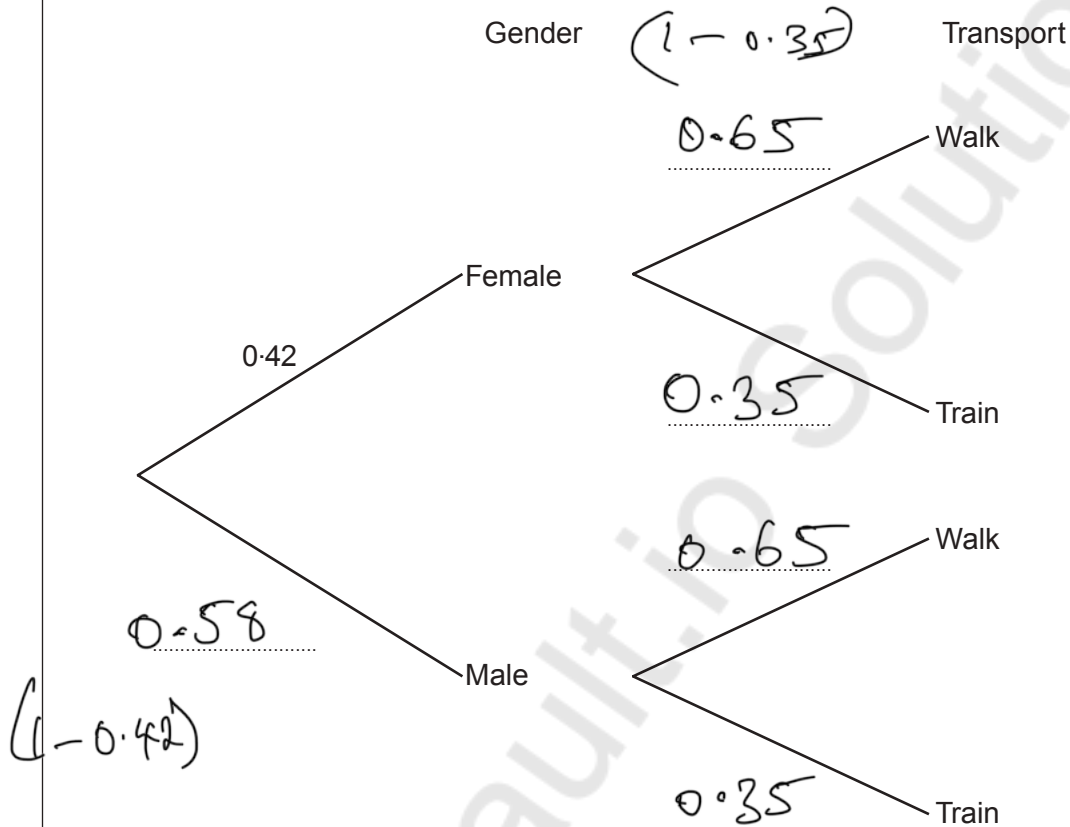
The probability that this person is female is 0.42.

The probability that this person took the train is 0.35.

The decision to walk or take the train is independent of gender.

- (a) Complete the tree diagram shown below.

[3]



- (b) The person chosen at random receives a gift voucher.  
What is the probability that this person is female and travelled up the mountain by train?

[2]

Probability of being female = 0.42

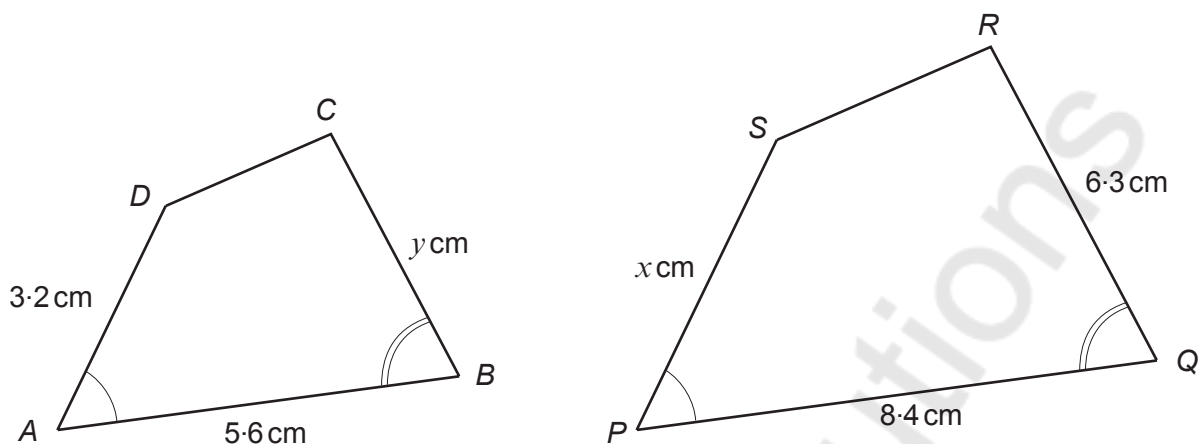
Probability of using train = 0.35

$$\text{Ans} = 0.42 \times 0.35$$

$$= 0.147$$



17. The diagrams below show two similar shapes,  $ABCD$  and  $PQRS$ .



Diagrams not drawn to scale

- (a) Calculate the value of  $x$ .

[2]

$$\frac{3.2}{x} = \frac{5.6}{8.4}$$

$$x = \frac{3.2 \times 8.4}{5.6}$$

$$= 4.8$$

- (b) Calculate the value of  $y$ .

[2]

$$\frac{y}{6.3} = \frac{5.6}{8.4}$$

$$y = \frac{6.3 \times 5.6}{8.4} = 4.2$$



(c) Explain clearly why the following statement cannot be true.

[2]

'The length of  $CD$  is 3.9 cm and the length of  $RS$  is 6.5 cm'.

$$\frac{3.9}{6.5} = 0.6$$

$$\frac{5.6}{8.4} = 0.67$$

So Comparison Shows that  $\frac{CD}{RS} \neq \frac{AB}{PQ}$

$\therefore$  The Statement is not true



18. A rectangle of length 12 cm and width  $(2x - y)$  cm has an area of  $72 \text{ cm}^2$ .

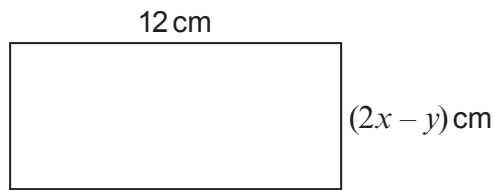


Diagram not drawn to scale

$KLMN$  is a kite where  $KL = 3x$  cm and  $LM = y$  cm.

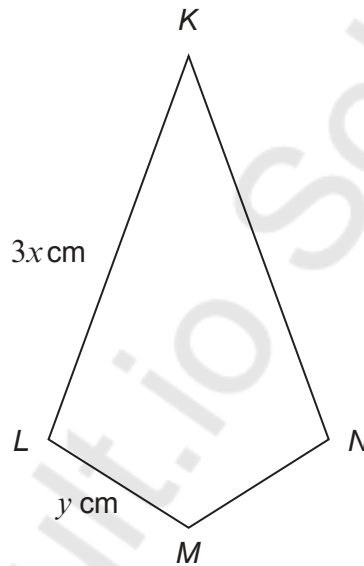


Diagram not drawn to scale

The perimeter of the kite  $KLMN = 33$  cm.

Calculate the values of  $x$  and  $y$ .

You must show all your working.

Do not use a trial and improvement method.

[5]

$$\begin{aligned} \text{Area of rectangle} &= l \times b \\ 12(2x - y) &= 72 \\ 24x - 12y &= 72 \\ 12(2x - y) &= 72 \\ 2x - y &= \frac{72}{12} \\ 2x - y &= 6 \end{aligned}$$



$$\text{Perimeter of kite} = 3x + 3x + y + y = 33$$

$$6x + 2y = 33$$

$$2(3x + y) = 33$$

$$3x + y = \frac{33}{2}$$

$$3x + y = 16.5$$

Solve as simultaneous equations

$$2x - y = 6$$

$$3x + y = 16.5$$

Add  
equations

$$5x = 22.5$$

$$x = \frac{22.5}{5}$$

$$x = 4.5$$

$$2x - y = 6$$

$$2(4.5) - y = 6$$

$$y = 9 - 6$$

$$y = 3 //$$



19.  $ABC$  and  $CDE$  are two right-angled triangles.

In triangle  $ABC$ ,  $AB = 6.5$  cm and  $BC = 10.4$  cm.  
In triangle  $CDE$ ,  $CE = 9.4$  cm.

$$\widehat{BCE} = 22^\circ.$$

$$\widehat{ACB} = x^\circ.$$

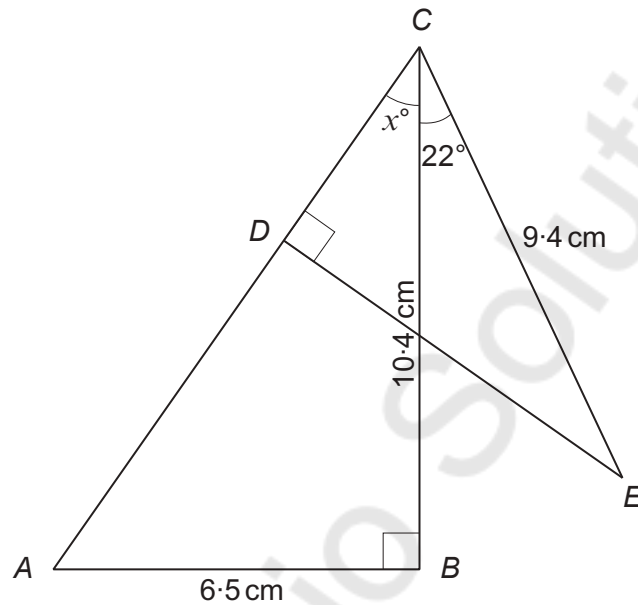


Diagram not drawn to scale

(a) Calculate the value of  $x$ .

[3]

To find  $x$  ∴  $\tan ACB = \frac{6.5}{10.4}$

$$\angle ACB = \tan^{-1}\left(\frac{6.5}{10.4}\right)$$

$$\angle ACB = 32^\circ$$

$$\therefore x = 32$$



(b) Hence find the length of  $DE$ .

[3]

$$DE = 9.4 \times \sin(22 + 32)$$
$$= 7.6 \text{ cm}$$

$$DE = \underline{\underline{7.6 \text{ cm}}}$$

END OF PAPER



Question number	Additional page, if required. Write the question number(s) in the left-hand margin.
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Examiner only

